## PERMAOEGLUMN。

## is <br> PERMA <br> COLUMN



- "The fermanent SqLutian"

Why should you have to choose between a foundation that is economical and one that is permanent PERMA-COLUMN5 ${ }^{\circ}$ are the first product to combine the econorny and speed of post-frame construction with the durability of a concretefoundation.

Proven - Concrete is the mest proven and durable foundation material known toman!

Economical - PERMA-COLUMNS are the most economical method of constructing a postframe bulliting on concrete!

Safo - PERMA-COLUMNS are safe and have no harsh chemicals or preservatives tike treated wood!

A building is onty as permanent as the foundation on which ft is built.

## What are you building on?



## Out with the old. <br> In with the new!

## The Permanent Solution For Rotten Posts

Introducing the new PERMA-COLUMN ${ }^{*}$ PC.6600. The same pre-cast technology available in new construction can now be used to repair rotten posts. Don't let deteriorated pasts compromise a building with many useful years left in It! The PC6600 is a tong awaited answer to an old and ongoing problem.

A building is only as permanent as the foundation on which it is bult.. Concrete... durable, economical, proven; it only makes sense to choose "The Permanent Solution." sales@permacolumn.com

# 1 PERMA 



## step-by step guide

1. Locate rotten post to be replaced. Detach siding and remove existing skirt board.
2. Dig down next to face and sides of rotten post with auger.
3. Support truss with brace and hydraulic jack.
4. Cut rotten post off at ground level. No measuring necessary at this point.

## 5. Remove rotten portion of post.

6. Clean out post hole to provide a level, compacted base for the pre-cast concrete pad. Sakrete or ready mix concrete can also be used for post base.
7. Install pad and measure the Perma-Column for exact clearance needed. "Note: Perma-Column length may vary.
8. Mark existing post and cut to desired clearance for PermaColumn installation.
9. Install and position Perma-Column.
10. Install $1 / 4^{\prime \prime} \times 3$ " wood lags. Drill and install (2) $1 / 2^{\prime \prime}$ bolts.

## 11. Reattach siding and skirt board.

Building ravoration is hewrdous and siould only be performed by a controdion proitsiphel. This gide in thentiretycan befoundon the what wwip pemacolumn.com


## TESTIMONIALS

When we firm saw the Perma-Columns, wa knew that was our cinower:"

"We have a 22 year old pole barm and had been watching the condition of the poles for roughly a year. Nothing appeared abnormal above ground, but when we dug the wooden poles out we found that nearly all of them were well over $50 \%$ gone. This was an accident waiting to happen.

When we first saw the Perma-Colurnns, wa knew that was our answer. They proved to be a cost and time effective means of solving our problem. Tocay we have a bullding, that in essence, has a concrete foundation with no wood in the ground."

Steve Cramer
Finciloy, OH
That much rot on fealed wood was sumpraing...

"We found that all the posts on our $100^{\circ} \times 110^{\prime}$ show arena were nearly or completely rotted off below the ground. That much rot on treated wood was surprising in a building that is just 20 years old. After we did the work, it's like we have a new building."

Tom Fultion
Huntington County Fair Board
Huritingion, iN

## 5 Maperib Ta Miser Yaum Mares

PC6300 -3 ply $2^{\prime \prime} \times 6^{\prime \prime}$ laminated wood column
PC6400 - 4 ply $2^{\prime \prime} \times 6^{n}$ laminated wood column
PC6600 - $8^{\prime \prime} \times 6^{\prime \prime}$ wood post and replacement
PC8300-3 ply $2^{\prime \prime} \times 8^{n \prime}$ laminated wood column
PC8400-4 ply $2^{n} \times 8^{n}$ laminated wood column
"Consult a design professional for appropratate model.
U๋
PERMA
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Why should you have to choose between a foundation that is economical and one that is permanent PERMA-COLUMN5 ${ }^{\circ}$ are the first product to combine the econorny and speed of post-frame construction with the durability of a concretefoundation.

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Safo - PERMA-COLUMNS are safe and have no harsh chemicals or preservatives tike treated wood!

A building is onty as permanent as the foundation on which ft is built.

## What are you building on?



## I．REVOLUTIONARY DESIGN

A．PERMA－COLUMNS are the first product to combine the economy of post－frame construction with the durablitity of a concrete foundation．
B．The exclusive design of the PERMA－COLUMN is patented．

## II．TECLHNICAL SPECIFICATIONS

A．The latest in SCC pre－casting technology creates a product with three times the strength of regular concrete．
B．Polymer fiber relinforcement and premfum grade steel reinforcement dramatically enhance flexural strength．
C．Corrosion inhibitors protect internal steel reinforcement．
D．Air entraining admixtures insure resistance to harsh freeze－ thaw cycles．

## III．INVESTMENT SECURITY

A．PERMA－COLUMNS ksep wood out of the ground ensuring that your building＇s foundation will never rot．
B．PERMA－COLUMNS protect your building investment by securing its value for a lifetime．

## IV．ENVIRONMENTAL SAFETY

A．PERMA－COLUMNS do not use the harsh chemicals found in treated lumber，which are being phased out by the EPA．
B．Using an environmentally frlendly product promotes peace of mind．

## V．STRENGTH DATA

A．PERMA－COLUMNS have been tested by The University of Wisconsin．Desisn manuals are available by request．
B．In comparative strength tests performed by Purdue University，PERMA－COLUNNS have proven to outperform the industry standard．


## 5 MロDELS Tロ MEET YロUR NEEDS



PC6300－for a 3 ply $2^{\prime \prime} \times 6^{n}$ Laminated wood column PC5 400 －for 14 ply $2^{\prime \prime} \times 6^{\prime \prime}$ laminated wood column PC6600－for a $6^{\prime \prime} \times 6^{\prime \prime}$ wood post replacement pceano－for a 3 ply $2^{\prime \prime}$ X $a^{\prime \prime}$ lamingted wood columin PCes 00 －for a 4 ply $2^{n} \times 8^{\prime \prime}$ laminated wood column Tonsile a dekty proferiknal for appropritate model．

## Installation Manual



THE PERMANENT SOLUTION

## Extreme Strength

Lasting Longevity
Environmentally Friendly


## FIVE MODELS TO MEET YOUR DESIGN REQUIREMENTS.

PC6300 - designed for a 3 ply $2^{\prime \prime}$ X 6 " laminated wood column ( $5^{\left.1 ⁄ 22^{\prime \prime} X 4 ½ \text { " }\right) ~}$
PC6400 - designed for a 4 ply $2^{\prime \prime}$ X 6 " laminated wood column ( $5 ½^{\prime \prime} \times 6$ ")
PC6600 - designed for a 6 " X 6 " wood post and replacement ( $51 / 2^{\prime \prime} \times 51 / 2^{\prime \prime}$ )
PC8300 - designed for a 3 ply $2^{\prime \prime} X 8$ " laminated wood column ( $71_{4} 4^{\prime \prime} X 4 \frac{1}{2} 2^{\prime \prime}$ )
PC8400 - designed for a 4 ply 2" X 8" laminated wood column ( $71 / 4$ " X 6")
Consult a design professional for appropriate model.

## Handling \& Storage

- Avoid direct impact of steel forks with concrete column to reduce surface chipping.
- Minor surface chipping can be repaired with premixed concrete patch available at your local hardware store.
- Place a wood spacer between every row of columns to avoid concrete to concrete contact. (A)
- Do not stack columns more than four rows high on a pallet. (A)
- Keep columns covered during storage and shipping to preserve appearance.
- PCs* can be dump unloaded by banding securely to wood bundle. (B)

*PERMA-COLUMN to be hereafter referred to as PC.


## Option 1: Preassembled Column

1. Place unassembled PC's close to the assembly table.
2. Assembly table to be level and no more that 12 " off the ground to facilitate manual lifting. (C) If a hoist is available, the assembly table works best at around 30" high.
3. A $2^{\prime \prime} \times 10$ " plank with a 2" $\times 4$ " back rail setting on cement blocks will suffice. (C)

4. Lift PC using a nylon "choke" strap around each end. (D)
5. Place PC on assembly table and insert wood column in steel bracket. may need to be square cut to insure tight fit. (E) tight during assembly. through wood column.

## Fastener Requirements*

(4) $1 / 4^{\prime \prime} \times 3^{\prime \prime} \quad$ Simpson ${ }^{\text {TM }}$ SDS screws (or equal) required for PC6300, PC 6400 and PC6600.
(8) $1 / 4^{\prime \prime} \times 3^{\prime \prime} \quad$ Simpson ${ }^{\text {TM }}$ SDS screws (or equal) required for PC8300 and PC8400.
(2) $1 / 2^{\prime \prime} \times 6^{\prime \prime} \quad$ Grade \#5 HHCS bolt, nut and washer required for PC6300 and PC8300.
(2) $1 / 2^{\prime \prime} \times 7^{\prime \prime} \quad$ Grade \#5 HHCS bolt, nut and washer required for PC6600.
(2) $1 / 2^{\prime \prime} \times 8^{\prime \prime} \quad$ Grade \#5 HHCS bolt, nut and washer required for PC6400 and PC8400.
*Fasteners are not provided.
8. Insert $1 / 2^{\prime \prime}$ grade 5 bolts in drilled holes and tighten nuts to approximately 110 foot pounds of torque.
9. Roll assembled column off the back side of the table onto wood stickers for skid loader pick-up.


## Option 2: Unassembled Column

- PC's can be installed without the wood upper, using the same procedures as the "Post Hole Digging Requirements" below.
- This will allow for better access to place the concrete floor. (F)
- Using this option allows for building to be started in the fall and completed in the winter.



## Attaching Uplift Anchors

20AU UPLIFT ANCHOR

1. Consult a design professional for appropriate sized uplift anchor.

PC20UA Uplift Anchor 2" $\times 2^{\prime \prime} \times 8.5^{\prime \prime}$ Galvanized
PC30UA Uplift Anchor 3" $\times 3^{\prime \prime} \times 12$ " Galvanized
2. Attach uplift anchor with $1 / 2^{\prime \prime}$ bolt. Tighten nut firmly until uplift anchor does not rotate.
$1 / 2^{\prime \prime} \times 7$ " bolt and nut required for PC6300, PC6400 and PC6600. $1 / 2^{\prime \prime} \times 9$ " bolt and nut required for PC8300 and PC8400.


## Post Hole Digging Requirements

- For required PC embedment depth, consult a design a professional.
- Concrete portion of PC's to be flush with the sidewall girt line.
- Overhead door openings to be $3^{\prime \prime}$ wider than desired finished opening to accommodate $11 / \mathbf{2}^{\prime \prime}$ PC bracket trim-out. (G)
- Slide door openings to be the same as the desired finished opening. PC brackets intrude into the slide door opening by 3/8". (H)
- Dig post hole depth so all PC brackets are at a uniform height. If adjustment is necessary, use tamped gravel.
- If bedrock is contacted at a post hole location, the bottom of the PC may be cut off using a masonry saw. The uplift anchor hole will need to be redrilled using a 9/16" masonry drill bit.


## OHD DOOR JAMB



## SLIDE DOOR JAMB

(H)


## Column Placement and Leveling

1. Attach a $3 / 8$ " wood filler to the (4) corner columns to make girts and skirt flush. (I)
2. Lift multiple PC assemblies with a skid loader and drive along the post hole line.
3. Place concrete pad in bottom of hole prior to setting PC. Consult design professional to determine thickness of concrete pad.
4. Tilt PC assemblies off skid loader forks into post hole. (J)
5. Plumb the PC columns using standard leveling procedures. (K)
6. Backfill post holes with appropriate materials, tamping 6 " layers until hole is filled.


## Skirt Board Attachment

1. Install first row of sidewall girts before attaching the skirtboard. The skirtboard will be hung from this first row of girts.

Make two skirt hangers to allow for hands free skirt placement. (L)

- Using a 2" $\times 4$ " board, cut the board to the proper length to hang the skirtboard.
- Attach a metal "C" bracket ( $11 / 2$ " pocket) to this board to hang over the bottom girt row.
- Attach a metal "L" bracket ( $11 / 2$ " seat) to this board to hang the skirtboard in place.

2. Hang the skirtboard from the first girt row using skirt hanger while drilling and attaching.
3. Drill a $3 / 16^{\prime \prime}$ hole through the skirt board and $2^{\prime \prime}$ into the concrete post using a hammer drill. (M)

NOTE: Angle the drill toward the center of the concrete post to avoid hitting the interior rebar. (E page 2)
4. Drive a $3 / 16^{\prime \prime} \times 3^{\prime \prime}$ Powers stainless steel split drive anchor (PC3DA-SS) into the post until the skirt is secure. (N)

(N)


## Porch Post Trim Detail

1. Porch posts can be trimmed-out using the following methods.


## METHOD 2



# Perma-Column Design and Use Guide for <br> PC6300, PC6400, PC6600, PC8300, and PC8400 Models 


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April 18, 2005

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## Foreword

The following Design and Use Guide for PC6300, PC6400, PC6600, PC8300, and PC8400 Models has been written by Brent Leatherman to help engineers apply information appearing in the Engineering Design Manual for Series 6300, 6400, 8300, 8400 PermaColumns. I wrote the latter document after conducting a number of tests on Perma-Columns in my laboratory at the University of Wisconsin-Madison. In addition to a summary of UW-Madison test results, the Engineering Design Manual contains details on how to calculate design properties for Perma-Columns. The Design and Use Guide reviews these procedures, and contains sample calculations and comparisons that you will not find in the Engineering Design Manual.

Perma-Columns are a more environmentallyfriendly alternative to preservative-treated wood, and quite likely, a more durable alternative. Using the information contained in this document and in the Engineering Design Manual, an engineer can better ensure the structural integrity and safety of buildings incorporating Perma-Columns.


## 1. Design Overview

This guide is intended to be used as a companion document to the Engineering Design Manual for Series 6300, 6400, 8300, 8400 Perma-Columns (herein referred to as "the Manual") by David R. Bohnhoff. Each Perma-Column assembly consists of a reinforced concrete base designed according to The American Concrete Institute (ACI), a steel bracket designed according to The American Institute of Steel Construction (AISC), and a mechanically laminated wood column designed according to The American Forest and Paper Association (AF\&PA) specifications. The structural analysis for each of these components was performed using a load and resistance factor (LRFD) design methodology. This was done to allow use of one set of load combinations for the entire assembly, and to provide an accurate look at column failure modes. The deflection limits used in this design were taken from IBC 2003 Table 1604.3 for exterior walls with brittle or flexible finishes, and are $\mathrm{L} / 240$ and $\mathrm{L} / 120$, respectively. The overall column deflection is to be checked using service (unfactored) loads.

This guide will cover properties, and design issues for the reinforced concrete base, the steel bracket connection, and the mechanically laminated wood columns. We will look at creating models of the Perma-Column assemblies to simulate the results of laboratory testing. Design charts will be presented for all the Perma-Column assemblies with varying heights, and boundary conditions. The failure modes and design limitations on each Perma-Column assembly will be discussed, and we will give an example showing a straight forward design approach which can be applied to all PermaColumn assemblies. Finally, we will look at wind uplift capacity for a concrete collar or a packed fill foundation condition.

## 2. Perma-Column Descriptions

Dimensions and material properties for the PC6300, PC6400, PC6600, PC8300, and PC8400 models are given in Table 2.1. The PC6600 model is intended for new or replacement solid-sawn $6 \times 6$ posts and was not included in the laboratory testing. Variable definitions correspond to Figure 1.1 of the Manual. Section properties for 3-ply 2x6, 4-ply 2x6, 3-ply 2x8, and 4-ply 2x8 mechanically laminated wood columns are given in Table 3.5.1 of the Manual.

Table 2.1: PC6300, PC6400, PC6600, PC8300, and PC8400 Dimensions and Properties


| Variable | Symbol | Units | PC6300 | PC6400 | PC8300 | PC8400 | PC6600 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Overall Concrete Width | $b$ | in. | 5.38 | 6.88 | 5.38 | 6.88 | 6.38 |
| Overall Concrete Depth | $\boldsymbol{h}$ | in. | 5.44 | 5.44 | 7.19 | 7.19 | 5.44 |
| Depth to Top Steel | $d^{\prime}$ | in. | 1.50 | 1.50 | 1.56 | 1.56 | 1.50 |
| Depth to Bottom Steel | $d$ | in. | 3.94 | 3.94 | 5.62 | 5.62 | 3.94 |
| Width of Steel Bracket | s1 | in. | 5.00 | 5.00 | 7.00 | 7.00 | 5.00 |
| Top \& Bottom Steel Spacing | s2 | in. | 2.44 | 2.44 | 4.06 | 4.06 | 2.44 |
| Steel Distance to Bracket Edge | s3 | in. | 1.28 | 1.28 | 1.47 | 1.47 | 1.28 |
| Area of Top Steel | $\boldsymbol{A s}^{\prime}{ }^{\prime}$ | in. ${ }^{2}$ | 0.40 | 0.40 | 0.62 | 0.62 | 0.40 |
| Area of Bottom Steel | $\boldsymbol{A}_{s}$ | in. ${ }^{2}$ | 0.40 | 0.40 | 0.62 | 0.62 | 0.40 |
| Steel Yield Strength | $f_{y}$ | $\mathrm{lbf} / \mathrm{in} .{ }^{2}$ | 60,000 | 60,000 | 60,000 | 60,000 | 60,000 |
| Concrete Compressive Strength (nominal) | $f_{c}{ }^{\prime}$ | $\mathrm{lbf} / \mathrm{in} .{ }^{2}$ | 10,000 | 10,000 | 10,000 | 10,000 | 10,000 |
| Steel Modulus of Elasticity | $\boldsymbol{E}_{s}$ | $\mathrm{lbf} / \mathrm{in} .{ }^{2}$ | 29000000 | 29000000 | 29000000 | 29000000 | 29000000 |

## 3. Reinforced Concrete Design

The reinforced concrete component is manufactured with $10,000 \mathrm{psi}$ (nominal) pre-cast concrete and four (4) 60,000 psi vertical reinforcing bars. Number 4 bars are used for the PC6300, PC6400, and PC6600, while number 5 bars are used for the PC8300, and PC8400 models. The required concrete cover for reinforcing bars in pre-cast concrete is lower because of better placement accuracy during the manufacturing process. The high concrete strength and quality is achieved by adding superplasticizers which increase strength by allowing a low water-to-cement ratio. Fiber reinforcers are added to reduce shrinkage, increase impact resistance, and increase flexural strength. Other admixtures are included in the concrete mix to increase freeze/thaw resistance, protect the steel reinforcement from rusting, increase flexural and compressive strength, and optimize the hydration process. Bending, axial and shear strength properties of the reinforced concrete are discussed in Section 3 of the Manual.

## 4. Steel Bracket Design

Figure 4.1 shows dimensions for the different steel brackets that are used with the Perma-Column assemblies. The brackets consist of $1 / 4$ " A36 steel with $5 / 8^{\prime \prime}$ diameter holes for the bolts, and $5 / 16$ " diameter holes for screws. The bracket connection utilizes $1 / 2^{\prime \prime}$ diameter A325 bolts in double shear with hex nuts torqued to $110 \mathrm{ft}-\mathrm{lbs}$, and $1 / 4 " \times 3$ " strong drive screws (SDS) by Simpson Strong-Tie or equivalent in single shear installed from each side. Typically, one screw is installed from each side of the bracket at each bolt, except the PC8300 and the PC8400 have two screws on each side at each bolt. Screws help prevent stress concentrations around the bolt which would cause splitting of the wood members. The wood columns bear directly on a $1 / 4$ " steel seat plate which helps to transfer axial loads directly into the concrete base. Four A706 weldable reinforcing bars are inserted in holes in the bottom of the bracket and fillet welded, connecting the bracket to the concrete base.


Pats Notes:
A $=1 / 4$ " steel bracket
$B=1 / 4$ " steel seat plate
$\mathrm{C}=5 / 8^{\prime \prime} \varnothing$ hole for bolt
$D=5 / 16^{\prime \prime} \varnothing$ hole for screw

PC6300


PO6400


PC8300
Figure 4.1 Steel Bracket Assemblies


POb60


PC8400

### 4.1 Bracket Moment Capacity

This joint has significant moment capacity and does not need to be modeled as a pin. The strength of the concrete-to-steel bracket, and the steel bracket-to-wood post connections needs to be evaluated in order to determine the moment capacity of the joint. The reinforcing bars transfer shear and moment between the concrete base and the steel bracket. The failure modes observed in the laboratory testing are 1.) concrete crushing and 2.) tension steel fracture (see Figure B. 5 and B. 6 in the Manual). The bolts and screws transfer shear and moment between the steel bracket and wood column. The fasteners themselves, and not the steel bracket, control the strength of this joint. The bolt and screw design should be performed according to the 1996 edition of the LFRD Manual for Engineered Wood Construction by The American Forest and Paper Association (AF\&PA).

### 4.2 Rotational Stiffness

The rotational stiffness of the steel bracket connection depends upon both concrete-to-steel, and steel-to-wood movement. Table B. 2 and Figure B. 4 in the Manual show joint rotation versus bending moment data for the steel bracket-to-concrete connection. The moment capacity of each steel bracket was chosen as $60 \%$ of the maximum tabulated value shown in Table B. 2 of the Manual. Table 4.1 shows the calculated stiffness values for the concrete-to-steel joint as discussed in Section 6.2 of the Manual. A linear assumption between joint rotation and bending moment was used to determine the rotational stiffness of each bracket. This stiffness value is needed in order to create a model as discussed in Section 6 of this Guide.

The stiffness of the steel-to-wood connection is controlled by the slip modulus for the bolts and screws, and is discussed in Section 6 of the Manual. The slip modulus should be assigned to the fastener group by summing the values of the individual fasteners in the group. The slip modulus for the $1 / 2$ " bolt in double shear is $85.5 \mathrm{k} / \mathrm{in}$, and for the screws is 28.7 kips per inch.

| Table 4.1 Element Strength and Stiffness Values |  |  |
| :--- | :--- | :---: |
| Series | Concrete-to-Steel <br> Stiffness (k-in/rad) | Ultimate Strength <br> (in-kip) |
| PC6300 | 2500 | 70.4 |
| PC6400 | 2523 | 70.9 |
| PC6600 | 2503 | 70.4 |
| PC8300 | 4815 | 123.9 |
| PC8400 | 4874 | 138.9 |

### 4.3 Friction

The moment capacity and rotational stiffness of the steel-to-wood joint is enhanced by friction produced when the bracket tends to pinch together as the bending moment increases. No increases were taken in the Manual for this phenomenon, but it remains as an additional safety factor against steel bracket-to-wood connection failure.

## 5. Mechanically Laminated Wood Column Design

The wood portion of a Perma-Column assembly is designed using LRFD because that is the preferred method of design for the steel and reinforced concrete components. Reference strengths for wood member sizing, and the factored resistance values for connection detailing are taken from the 1996 edition of the LFRD Manual for Engineered Wood Construction by AF\&PA. Design procedures were
taken from ASAE EP559 Design Requirements and Bending Properties for Mechanically Laminated Columns and from The LFRD Manual. No wet service reductions have been used since the wood portion is not in contact with the soil or concrete, and it is assumed to be used in an enclosed building. There are no splices in the wood laminations. Axial load is assumed to be transferred by direct bearing on the seat plate, and not through bolts or screws. Buckling length for bending about the strong axis is one foot less than the overall column height because the concrete portion extends one foot above grade. The corresponding effective buckling length factor, Ke , was conservatively taken as 1.2 for columns fixed at the base, with horizontal movement allowed at the top; and 0.8 for columns pinned at the top. Structural analyses were performed using \#1 Southern Yellow Pine (SYP), and \#2 Spruce Pine Fir (SPF). The \#1 SYP Nail-Lam "Plus" column as manufactured by Ohio Timberland Products, Inc was also included. More wood species and column assemblies will be checked in the future.

## 6. Modeling

Figure 6.1 shows an example of the structural analogs that were used to check each Perma-Column assembly. The structural analysis was performed using Frame Analysis and Design by Digital Canal, Inc. The structural analog was created with element stiffness values that closely simulate laboratory test results. These structural analogs can be used to predict Perma-Column assembly behavior under many different load conditions. The concrete element for each Perma-Column model was created using a concrete modulus of elasticity $\mathrm{E}_{\mathrm{c}}$, of 5.7 million psi, and an effective moment of inertia, $\mathrm{I}_{\mathrm{e}}$, as given in Table 5.2.1 in the Manual. I for the PC6600 was taken as $30 \mathrm{in}^{4}$ for modeling purposes. Elements 1, 2, and 3 of the analogs shown in Figure 6.1 represent the reinforced concrete base.

Element 4 in the analog represents the steel bracket. The purpose of this element is to model the bending flexibility of the steel bracket where it attached to the concrete. This element was assigned a modulus of elasticity, Es of 29 million psi, an effective length Le of 2.5 inches, and an effective moment of inertia I equal to $S(\mathrm{Le}) / E s$ where $S$ is the rotational stiffness from Table 4.1. Table 6.1 summarizes the moment of inertia used for the concrete and steel bracket elements.


8300-16-0 Analog
Figure 6.1 Structural analogs for a column with pin or spring at top

| Table 6.1 Element Moment of Inertia Values (in ${ }^{\mathbf{4}}$ ) |  |  |  |
| :--- | :--- | :--- | :--- |
| Series | Concrete Element (Ie) | Concrete-to- <br> Steel <br> Element (I) | Steel-to- <br> Wood <br> Element (I) |
| PC6300 | 25.4 | 0.215 | 1.26 |
| PC6400 | 38.7 | 0.218 | 5.41 |
| PC6600 | 30 | 0.216 | 1.26 |
| PC8300 | 72.2 | 0.415 | 4.6 |
| PC8400 | 88.3 | 0.420 | 4.6 |

Element 5 in the analog is used to model the bracket-to-wood connection. This element extends between the fastener groups, and models the rotation between steel and wood. The length varies depending on the centroid of the fastener group. 8 inches was used for the PC6300 and PC6600, 13 inches for PC6400, and 11 inches for PC8300 and PC8400 (see Figure 4.1).

Elements 6 and 7 in the analog represent the laminated wood column with an $E$ value of 1.7 million psi for \# 1 SYP, and 1.4 million psi for \#2 SPF.

After the structural analog was created and the loading applied, a P-delta analysis was performed to account for increased section forces induced by column deflection. Three post models were analyzed for each height to simulate different boundary conditions at the eave. The first assumes a very rigid diaphragm which allows no horizontal movement at the eave. The second and third models allow a horizontal movement corresponding to $\mathrm{L} / 240$ and $\mathrm{L} / 120$ respectively. These eave displacements were evaluated using service loads, and the larger of sidesway or curvature was taken as the controlling value. Horizontal movement was created in the model by using a spring support in place of a roller support. The post foundation was modeled assuming a $4^{\prime}-0^{\prime \prime}$ embedment depth. A pin was used at the bottom, and a vertical roller at $1 / 3$ the embedment depth to simulate a non-constrained post foundation.

## 7. Perma-Column Design Charts

Table 7.1 shows the maximum factored vertical load, $\mathrm{P}_{\mathrm{u}}$, for Perma-Column assemblies under a constant wind load of 120 pounds per lineal foot. The post heights evaluated range from $8^{\prime}-0$ " up to $20^{\prime}-0$ " in two foot increments. Blank boxes in the chart indicate the column fails in deflection due to the constant wind load. Gray shaded numbers indicate Perma-Column assemblies limited by the steel bracket capacity. The failure modes checked are as follows:

1. Deflection Due to Service Loads
2. Wood Elements
a. Combined axial and bending moment
b. Shear
3. Steel Bracket Element
a. Bending moment at base
4. Bracket-to-Wood Connection Element
a. Combined shear and bending moment on steel-to-wood connection
5. Concrete Elements
a. Bending moment and axial force compared to Interaction Diagram in Figure 3.3.2 in the Manual
b. Shear
Table 7.1 Perma-Column Design Chart
Maximum factored vertical load, Pu (kips), for Perma-Column assemblies under constant wind load

| \#1 SYP | Column Height (ft) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 8 |  |  | 10 |  |  | 12 |  |  | 14 |  |  | 16 |  |  | 18 |  |  | 20 |  |  |
| Eave Condition | I | II | III | I | II | III | I | II | III | 1 | II | III | 1 | II | III | 1 | II | III | 1 | II | III |
| Eave Deflection (in) | 0 | 0.8 | 0.4 | 0 | 1 | 0.5 | 0 | 1.2 | 0.6 | 0 | 1.4 | 0.7 | 0 | 1.6 | 0.8 | 0 | 1.8 | 0.9 | 0 | 2 | 1 |
| PC6600 $6 x 6$ <br> P  | 38 | 33 | 33 | 32 | 24.6 |  | 24 | 16.2 |  | 17 |  |  |  |  |  |  |  |  |  |  |  |
| PC6300 3 3 ply x 6 | 56 | 33.6 | 33.6 | 42 | 23.4 | 23.4 | 29 | 16.8 | 16.8 | 19 | 10.8 |  | 13 | 5.4 |  |  |  |  |  |  |  |
| PC6400 4 4 ply x 6 | 75 | 45 | 45 | 58 | 31.8 | 31.8 | 42 | 22.8 | 22.8 | 29 | 16.8 |  | 20 | 12 |  | 15 |  |  |  |  |  |
| PC8300 3 3 ply x 8 | 80 | 63 | 63 | 70 | 48 | 48 | 60 | 36 | 36 | 41 | 27.6 | 27.6 | 34 | 21.6 | 21.6 | 26 | 15 | 15 | 19 |  |  |
| PC8400 4 ply x 8 | 100 | 63 | 63 | 90 | 63 | 63 | 80 | 48 | 48 | 64 | 36 | 36 | 49 | 29.4 | 29.4 | 38 | 23.4 | 23.4 | 29 | 9 |  |
| Ohio Timberland Nail-Lam "Plus" |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | 57 | 35 | 35 | 41.5 | 20.5 | 20.5 | 27.5 | 12.8 | 12.8 | 20.3 | 9.3 |  | 12 | 5.4 |  |  |  |  |  |  |  |
| PC6400 4 4 ply x 6 | 78.8 | 49 | 49 | 58.6 | 29 | 29 | 40 | 18.6 | 18.6 | 27.2 | 12.4 |  | 18.7 | 8.4 |  | 13.8 |  |  |  |  |  |
| PC8300 3 3 ply x 8 | 84 | 72.6 | 72.6 | 79 | 54.5 | 54.5 | 63.9 | 34.6 | 36.6 | 43.3 | 23.6 | 23.6 | 35.4 | 16.4 | 16.4 | 27.2 | 12.4 | 12.4 | 20 |  |  |
| PC8400 4 4 ply x 8 | 114 | 98.6 | 98.6 | 104 | 71 | 71 | 89 | 48.7 | 48.7 | 69.2 | 33.8 | 33.8 | 51.5 | 24 | 24 | 39.6 | 18 | 18 | 30.4 | 9 |  |
| Comparison to typical pressure treated wood columns |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | Column Height (ft) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  | 8 |  |  | 10 |  |  | 12 |  |  | 14 |  |  | 16 |  |  | 18 |  |  | 20 |  |
| Eave Condition | I | II | III | I | II | III | I | II | III | I | II | III | I | II | III | I | II | III | I | II | III |
| Eave Deflection (in) | 0 | 0.8 | 0.4 | 0 | 1 | 0.5 | 0 | 1.2 | 0.6 | 0 | 1.4 | 0.7 | 0 | 1.6 | 0.8 | 0 | 1.8 | 0.9 | 0 | 2 | 1 |
| 6x6 \#2 trd SYP | 21 | 21 | 21 | 16 | 10.8 | 10.8 | 11 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 3 ply x 6 trd. \#1 SYP* | 41 | 30 | 30 | 38 | 20.4 | 20.4 | 19 | 12 | 12 | 13 | 5.7 |  | 8 |  |  |  |  |  |  |  |  |
| * Non-spliced |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| \#2 SPF | Column Height (ft) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | 8 |  |  | 10 |  |  | 12 |  |  | 14 |  |  | 16 |  |  | 18 |  |  | 20 |  |  |
| Eave Condition | 1 | II | III | I | II | III | I | II | III | 1 | II | III | 1 | II | III | 1 | II | III | 1 | II | III |
| Eave Deflection (in) | 0 | 0.8 | 0.4 | 0 | 1 | 0.5 | 0 | 1.2 | 0.6 | 0 | 1.4 | 0.7 | 0 | 1.6 | 0.8 | 0 | 1.8 | 0.9 | 0 | 2 | 1 |
| PC6300 3 3 ply x 6 | 48 | 26.4 | 26.4 | 27 | 17.4 | 17.4 | 18 | 8.4 | 8.4 | 11 | 1.5 |  |  |  |  |  |  |  |  |  |  |
| PC6400 4 4 ply $\times 6$ | 49 | 33 | 33 | 38 | 24.6 | 24.6 | 27 | 16.8 | 16.8 | 18 | 7.8 |  | 11 | 1.8 |  |  |  |  |  |  |  |

[^0]The notes at the bottom of the chart describe the assumptions and conditions to which these maximum vertical loads apply. This chart assumes columns with full lateral bracing and only major axis bending. It is also important to note that the structural analogs used to create these charts have a support at the top of the post to simulate resistance to horizontal loads due to diaphragm action. The Perma-Column assemblies are not designed for "flagpole" situations where no support at the top of the posts can be expected. Additional wind bracing or kneebraces may need to be added to the overall building design if no diaphragm resistance is present. This is especially important to keep in mind when using the PC6600 as a replacement post. The overall building design should be evaluated to verify that the replacement post is adequate.

The chart shows that the main controlling factors in the design are the imposed deflection limits, and the strength of the wood portion of the column. The bracket connection to the wood post controls the design for the $20^{\prime}$ high, condition 2 only. A comparison to a $\mathbf{6 x 6} \# 2$ treated column, and a 3 ply $2 \times 6$ \#1 treated non-spliced column using the same wind load and same boundary conditions is shown. The PC6300 performs significantly better than its 3 ply $2 \times 6$ treated counterpart mainly because it has no wet service reduction, and the maximum bending moment is resisted by the concrete component below grade. Updating this chart with an effective buckling length factor, Ke , of 1.0 for conditions II and III may better represent the actual behavior of the columns in the field, and would give better performance overall.

## 8. Design Example

This design example is for a PC8300 with a 3 ply $2 \times 6$ \#1 Southern Pine laminated wood column. The column is 16 ' high and the eave is allowed to deflect horizontally 1.6 " ( $\mathrm{L} / 120$ ). The vertical load is 2.8 kips dead load, and 8.4 kips snow load. The horizontal loading is 120 pounds per foot due to wind load. All assumptions listed in the chart apply to this example, as does the structural analog with a spring shown in Figure 6.1. This is a summary of the design process; the detailed calculations are available in the Appendices to this document.
8.1 The controlling load combinations for the given dead, snow, and wind loading are as follows

1) $\mathrm{D}+\mathrm{W}$ (Service loads for deflection check)
2) $1.2 \mathrm{D}+1.6 \mathrm{~S}+0.8 \mathrm{~W}$
3) $1.2 \mathrm{D}+0.5 \mathrm{~S}+1.6 \mathrm{~W}$
4) $0.9 \mathrm{D}+1.6 \mathrm{~W}$
8.2 The column is analyzed for the given loading and the failure modes checked as outlined in Section 7 above.
8.2.1 Deflection due to service loads Actual deflections are within allowable of $16(12) / 120=1.6 \quad$ OK
8.2.2 The factored internal forces in the wood elements are $\mathrm{M}_{\mathrm{ux}}=25$ inch-kips and $\mathrm{Pu}=$ 16.8 kips for load combination 2, and $\mathrm{M}_{\mathrm{ux}}=60$ inch-kips and $\mathrm{Pu}=6.5$ kips for load combination 3.
8.2.2.1 The interaction value in the combined axial force and bending moment check is .96 for load combination 2 , and 0.49 for load combination 3 . $0.91<1.0$

OK
8.2.2.2 The design shear strength of a 3 ply $2 \times 8$ SYP member is 8.5 kips . The factored shear is 1.5 kips.


Shear Diagram
(Comb 3)


Moment Diagram
(Comb 3)

Figure 8.1 Shear and Moment diagram for PC8300, 16' high with 1.6" maximum deflection under load combination 3

### 8.2.3 Steel Bracket Element

8.2.3.1 The maximum factored bending moment at the bottom of the steel bracket is 37.7 inch-kips compared to the chosen allowable moment of 74.34 inch-kips from Table B. 2 in the Manual
8.2.4 Bracket-to-Wood Connection Element
8.2.4.1 The combined shear and bending moment on the connection produce an equal and opposite force on the top and bottom fastener groups. The factored shear is 1.5 kips , and the average factored moment is 28.85 inch-kips. These combine to produce a resultant load of 4.2 kips on each fastener group assuming a distance of 11 inches between the centroid of each group. The maximum allowed connection force due to factored loads is 4.7 kips .

OK

### 8.2.5 Concrete Elements

8.2.5.1 The maximum factored bending moment below grade under load combination 3 is 92 inch-kips along with a factored axial force of 10 kips. These are well within the allowable envelope for the PC8300 when compared to the Interaction Diagram in Figure 3.3.2 in the Manual.
8.2.5.2 The minimum design shear strength of the PC8300 as given in Table 3.4.1 of the Manual is 4.5 kips . The factored shear in this example problem is 3.1 kips . OK

This column is adequate for the design loading.

## 9. Wind Uplift Capacity

Figure 9.1 shows two foundation conditions that may be used with a Perma-Column. The wind uplift capacity can be evaluated for each foundation condition using the procedure described in ANSI/ASAE EP486.1 October 2000 Shallow Post Foundation Design. The uplift calculations in this section follow the allowable stress design equations of EP486.1, and therefore are unfactored capacities. They should be compared with unfactored net uplift values to determine adequacy for a particular situation. Upward movement of a Perma-Column post foundation cannot occur without displacing a cone of soil as defined below.

For circular footings and collars:
Circular cast-in place concrete collars displace a conically shaped wedge of soil. The potential resistance of a circular collar, including soil and attached concrete, can be calculated from the following equation:
$U=\alpha G\left[0.33 \pi\left\{[(d-t)+0.5 w / \tan \theta]^{3}(\tan \theta)^{2}-0.125 w^{3} / \tan \theta\right\}-A_{p}(d-t)\right]+0.25 C \pi w^{2} t G$ Source:
ANSI/ASAE EP486.1 OCT00: Shallow Post Foundation Design

```
where:
U = soil and foundation uplift resistance, kN (lbf)
\alpha= soil density, kg/m}\mp@subsup{}{}{3}(85\textrm{lb}/\mp@subsup{\textrm{ft}}{}{3}
C = presumed concrete density, 90 kg/m
G = gravitational constant, 1 lbf/lbm (9.81N/kg)
d = embedment depth, m (4 ft)
t = collar thickness, m (1 ft)
w = collar width, m (ft)
```

For rectangular footings and collars:
Angle plates are fastened to the post displacing a round corner, truncated prismatic wedge of soil radiating above the angle plates. The uplift resistance from the mass of the truncated prismatic volume is calculated by the following equation:
$U=\alpha G\left[\left(w l-A_{p}\right)(d-t)+(w+l)(d-t)^{2} \tan \theta+0.33 \pi(d-t)^{2} \tan ^{2} \theta\right]$
Source: ANSI/ASAE EP486.1 OCT00: Shallow Post Foundation Design
where:
$\mathrm{U}=$ soil uplift resistance, kN (lbf)
$\alpha=$ soil density, $\mathrm{kg} / \mathrm{m}^{3}\left(\mathrm{lb} / \mathrm{ft}^{3}\right)$
$\mathrm{G}=$ gravitational constant, $1 \mathrm{lbf} / \mathrm{lbm}(9.81 \mathrm{~N} / \mathrm{kg})$
$\mathrm{d}=$ embedment depth, m (ft)
$\mathrm{t}=$ steel collar thickness, m ( ft )
$\mathrm{w}=$ width of collar, $\mathrm{m}(\mathrm{ft})$
1 = length of collar, $m$ ( ft )
$\mathrm{A}_{\mathrm{p}}=$ post cross sectional area, $\mathrm{m}^{2}\left(\mathrm{ft}^{2}\right)$
$\theta=$ soil friction angle, 26 deg


Standard Design
Alternative Design

## Figure 9.1 Foundation Details

Table 9.1 shows the wind uplift capacity in pounds for these foundation conditions:

1. 18" diameter concrete collar with $1 / 2^{\prime \prime} \times 12^{\prime \prime}$ reinforcing bar through Perma-Column
2. 24 " diameter concrete collar with $1 / 2$ " $\times 18^{\prime \prime}$ reinforcing through Perma-Column
3. $2 \times 2 \times 81 / 2 \times 0.134 "$ galvanized steel anchor with packed fill around posts
4. $2 \times 2 \times 12 \times 0.134$ " galvanized steel anchor with packed fill around posts

Table 9.1 Allowable Unfactored Uplift*

| PermaColumn | Concrete Collar |  | Uplift Angle |  |
| :--- | :---: | :---: | :---: | :---: |
|  | $\mathbf{1 8} \boldsymbol{\prime}$ | $\mathbf{2 4} \boldsymbol{\prime}$ | $\mathbf{2 x 2 x 8} \mathbf{1 / 2}$ | $\mathbf{2 x 2 \times 1 2}$ |
| PC6300 | 2272 | 3253 | 1908 | 2693 |
| PC6400 | 2257 | 3238 | 2004 | 2789 |
| PC6600 | 2262 | 3243 | 1972 | 2757 |
| PC8300 | 2255 | 3236 | 2005 | 2790 |
| PC8400 | 2236 | 3217 | 2102 | 2887 |

* Units are in pounds (lb)

The values in the chart are all limited by the weight of the soil cone. The shear strength of a $1 / 2$ " Grade 2 bolt (ASTM A307 bolt) is 10.0 ksi as published by the AISC Ninth Edition ASD Construction Manual Table J3.2. A $1 / 2$ " bolt has a cross sectional area of 0.196 in $^{2}$, thus a Grade 2 bolt in double shear will resist 3.92 kips ( 3920 pounds). The uplift angles are analyzed as a cantilever with a unit load at the midspan. The maximum uplift is calculated by the equation: $\mathrm{P}_{\text {allow }}=\left(\mathrm{S}_{\mathrm{x}} \mathrm{F}_{\mathrm{b}}\right) /(\mathrm{L} / 2) \quad(\mathrm{See}$ calculation and Fig 9.2 below).


## 10. Summary and Conclusion

Perma-Column assemblies consist of wood, steel, and reinforced concrete elements, and should be designed using LRFD. The PC6600 is not included in the Manual, but can be expected to perform between the PC6300 and the PC6400 models. New technologies with Self Compacting Concrete (SCC) make it possible to manufacture a high quality product through the use of superplasticizers and a low water to cement ratio. The 10,000 psi (nominal) compressive strength protects the reinforcing bars by limiting chips and cracks during handling, and also by reducing the effect of freeze-thaw cycles. Steel bracket can be designed as a moment connection if the structural analog accurately models the rotational stiffness from the laboratory testing for the concrete-to-steel and steel-to-wood connections. The wood portion of the Perma-Column assemblies can be any grade or species of lumber; however, this Guide only deals with \#1 SYP, the \#1 SYP Nail-Lam "Plus" column as manufactured by Ohio Timberland Products, Inc, and \#2 SPF. The effective length factor, Ke, for buckling was conservatively taken as 1.2 for columns fixed at the base, with horizontal movement allowed at the top (conditions II and III); and 0.8 for columns pinned at the top (condition I). Using an effective buckling length factor, Ke , of 1.0 for conditions II and III may better represent the actual behavior of the columns in the field, and would give better performance overall.

Each Perma-Column component can be modeled using a structural analog with properties corresponding to the results of the laboratory testing, and can be used to simulate the Perma-Column behavior under many other load conditions. The design charts in this Guide show that the PermaColumn assemblies are limited primarily by overall deflection, and by strength of the laminated wood members. The steel bracket connection to the wood component may be a limiting factor for tall columns under high wind loads. The Perma-Column assemblies perform significantly better than typical mechanically laminated wood columns under the same boundary conditions mainly because they have no wet service reduction, and the maximum bending moment is resisted by the concrete component below grade. The steel bracket and the reinforced concrete base did not control under the design conditions presented in this Guide. There are several foundation detail options including concrete collars and steel uplift angles that can be used with a Perma-Column to achieve adequate uplift resistance for most applications.

PERMA COLUMN POST SIZE CHART TO BE USED FOR ESTIMATING PURPOSES ONLY
CONDITIONS：DLINCR 1．2，LL INCR 1．6， 90 MPH WL，BLDG LE

 12＇UNDER TRUSS 14＇UNDER TRUSS
3 PLY X $6 \# 2$ SP 14＇
3 PLY X 6 \＃ 2 SP 14＇
3 PLY X 6 \＃ 2 SP 14＇

$\underset{\sim}{\sim} \underset{\sim}{\sim} \underset{\sim}{\sim}$ 3 PLYX 6 \＃ 2 SPF
3 PLY X 6 \＃ 2 SPF







号

 11.07 KIPS
11.49 KIPS









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 4 PLY X 6 \＃ 1 SYP $144^{\prime}$
 4 PLY X6\＃1 SYP 14
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\＃\＃\＃ 3 PLYX6\＃1SYP $=4$ PLYX6\＃2 SPF MAY ALSO BE UTILIZED


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## PERMA COLUMN POST SIZE CHART


3 PLY X 8 \＃ 1 SYP 20＇
3 PLY X 8 \＃ 1 SYP 20＇
3 PLY X 8 \＃ 1 SYP 20＇
3 PLY X 8 \＃ 1 SYP 20＇
3 PLY X 8 \＃ 1 SYP 20＇




$\underset{\sim}{\sim} \underset{\sim}{\sim} \underset{\sim}{\sim} \underset{\sim}{\sim}$ .20 KIPS
68 KIPS
16 KIPS
64 KIPS
12 KIPS

 3 PLY X 6 \＃ 2 SPF 10＇

 3 PLY X 6 \＃ 2 SPF 10＇



 3 PLY X 6 \＃ 2 SPF 10＇ 9．60 KIPS


2．00 KIPS

 6．80 KIPS 3 PLY X 6 \＃ 2 SPF $10^{\prime}$

 18．24 KIPS 3 PLYX 6 \＃ 2 SPF $10^{\prime}$











 3 PLY X 8 \＃ 1 SYP 16＇


 4 PLY X6\＃ 1 SYP $14^{\prime}$






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 3 PLYX6\＃1SYP＝ 4 PLYX6\＃2 SPF MAY ALSO BE UTILIZED

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## PERMA COLUMN POST SIZE CHART

| TOTAL ROOF LOAD | $\begin{gathered} \text { TO BE } \\ \text { CONDITIO } \end{gathered}$ | SED FOR ESTIMAT <br> DLINCR 1．2，LLINC | G PURPOSES ONL <br> 1．6， 90 MPH WL，BLD | $\begin{array}{r} \text { ENG } \\ \text { NGTH NOT TO EXCEE } \end{array}$ | EER OF RECORD $21 / 2$ TIMES WIDTH， | QUIRED OST DEPTH |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | $10^{\prime}$ UNDER TRUSS | $1{ }^{1}$＇UNDER TRUSS | 14 UNDER TRUSS | $16^{\prime}$ UNDER TRUSS | 18 ＇UNDER TRUSS | $20^{\prime}$ UNDER TRUSS |
| 7.30 KIPS | 3 PLY X6\＃2 SPF 10＇ | 3PLYX6\＃2SP12＇ | $3 \mathrm{PLY} \mathrm{X6} \mathrm{\# 2SP14}$ | 3 PLYX6\＃1 SYP 16＇ | $4 \mathrm{PLYX6} \mathrm{\# 1} 1$ SYP $18{ }^{\prime}$ | $3 \mathrm{PLY} \times 8$ \＃ 1 SYP 20 |
| 7.90 KIPS | 3 PLY $\times 6 \# 2$ SPF 10 $0^{\circ}$ | 3 PLYX6\＃2SP12＇ | 3 PLY $\times 6$ \＃ 2 SP 14 | 3 PLYX6\＃1 SYP 16＇ | $4 \mathrm{PLY} \times 6 \# 1$ SYP $18{ }^{\prime}$ | 3 PLY X8\＃1 1 SYP 20 |
| 8.51 KIPS | 3 PLY X6\＃ 2 SPF 10＇ | 3 PLYX6\＃2SP12＇ | 3 PLY X6\＃ 2 SP 14 | 3 PLYX6\＃1 SYP 16＇ | 4 PLY X6\＃1 1 SYP 1 | $3 \mathrm{PLYX8} \mathrm{\# 1} 1$ SYP 20 |


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3 PLY X 6 \＃ 2 SP 14＇
3 PLY X 6 \＃ 1 SYP 14＇

4 PLY X 6 \＃ 1 SYP 18＇
4 PLY X 6 \＃ 1 SYP 18＇
4 PLY X 6 \＃ 1 SYP 18＇
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4 PLY X 6 \＃ 1 SYP 18＇



3 PLY X6 \＃\＃ 2 SPF 12＇
3 PLY Y $6 \# 2$ SPF 12






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##  <br> 3 PLY X6 \＃ 1 SYP $=4$ PLYX6\＃2SPF MAY ALSO BE UTILIZED PLYX6\＃1 SYP

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# Engineering Design Manual for 

Series 6300, 6400, 8300, 8400 Perma-Columns

by<br>David R. Bohnhoff, Ph.D., P.E.<br>Professor, Biological Systems Engineering University of Wisconsin-Madison

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#### Abstract

Elements of a Perma-Column, like elements of any structural component or system, must be checked to ensure that loads applied to the building do not overload the column. In the case of a Perma-Column, three items must be checked for structural adequacy: the reinforced concrete portion, the steel bracket, and the connection between the steel bracket and a wood post. In the following document, design values for the reinforced concrete portion and steel bracket are presented.


## Disclaimer

Engineers using the Perma-Columns design values presented in this document must make sure that they are applicable to the condition in question. This document does not address load cases involving tension, bi-axial bending, torsion, or magnified moments as defined in ACI 318.

## 1. Perma Column Dimensions and Material Properties

Perma-column dimensions are graphical defined in Figure 1.1 and numerically compiled in Table 1.1. All dimensions identified in figure 1.1 except $\boldsymbol{s} 5$ remain fixed along the entire length of a Perma-column. This change does not impact axial, shear, or strong axis bending properties.


Figure 1.1. Variable definitions for Perma-columns.
Table 1.1: Perma Column Cross-Sectional Dimensions and Material Properties

| Variable | Symbol | Units | PC6300 | PC6400 | PC8300 | PC8400 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Overall Concrete Width | $b$ | in. | 5.38 | 6.88 | 5.38 | 6.88 |
| Overall Concrete Depth | $\boldsymbol{h}$ | in. | 5.44 | 5.44 | 7.19 | 7.19 |
| Depth to Top Steel | $d^{\prime}$ | in. | 1.50 | 1.50 | 1.56 | 1.56 |
| Depth to Bottom Steel | $d$ | in. | 3.94 | 3.94 | 5.62 | 5.62 |
| Width of Steel Bracket | s1 | in. | 5.00 | 5.00 | 7.00 | 7.00 |
| Top \& Bottom Steel Spacing | s2 | in. | 2.44 | 2.44 | 4.06 | 4.06 |
| Steel Distance to Bracket Edge | s3 | in. | 1.28 | 1.28 | 1.47 | 1.47 |
| Area of Top Steel | $A_{s}{ }^{\prime}$ | in. ${ }^{2}$ | 0.40 | 0.40 | 0.62 | 0.62 |
| Area of Bottom Steel | $\boldsymbol{A}_{s}$ | in. ${ }^{2}$ | 0.40 | 0.40 | 0.62 | 0.62 |
| Steel Yield Strength | $\boldsymbol{f}_{\boldsymbol{y}}$ | $\mathrm{lbf} / \mathrm{in} .{ }^{2}$ | 60000 | 60000 | 60000 | 60000 |
| Concrete Compressive Strength | $f_{c}{ }^{\prime}$ | $\mathrm{lbf} / \mathrm{in} .{ }^{2}$ | 10000 | 10000 | 10000 | 10000 |
| Steel Modulus of Elasticity | $\boldsymbol{E}_{s}$ | $\mathrm{lbf} / \mathrm{in} .{ }^{2}$ | 29000000 | 29000000 | 29000000 | 29000000 |

American Concrete Institute (ACI) specifications for concrete protection of steel reinforcement require that where precast concrete components will be exposed to earth or weather, a minimum concrete cover of 1.25 inches is required on all steel reinforcement (ACI 318 Section 7.7.2). Nominal concrete cover on steel in all Perma-Columns is 1.25 inches.

## 2. Design Overview

One of the primary tasks of the design engineer is to ensure that structural components are not overloaded. This is a fairly systematic process that involves three major steps: establishment of design loads, structural analysis and component selection.
During the first step - establishment of design loads - the engineer must estimate the actual maximum loads (a.k.a. extreme loads) that could be applied to the structure during its design life. These estimated loads are more generally known as nominal loads, but may also be referred to as service loads, working loads or unfactored loads. Common load categories include: dead, earthquake, fluid, soil, live, roof live, rain, snow, self-straining and wind. Note that in addition to estimating these loads, an engineer must select the various combination(s) of these loads that will be applied to the structure during the structural analysis phase.

Structural analysis, which is the second step in a design process, involves determining the forces induced in structural components when loads are applied to the structure. The simplicity of many structures enables engineers to limit most analyses to what is occurring within a given plane of the structure. Referred to as a two-dimensional analysis, such an investigation typically provides the engineer with the axial force, bending moment and shear force at every point of each component lying within the plane of interest.

The third and final step in the design process is to check that the axial force, bending moment and shear forces induced in each component do not exceed allowable values. Where the allowable strength of a component is exceeded, the component must be replaced with one that is more substantial, or other changes must be made to the structure to reduce the forces induced in the component. Regardless of which route is taken, the structure must typically be reanalyzed once changes are made to one or more components.
Critically important in the design process is to ensure that there is a sufficient margin of safety built into the design. Exactly how safety is "built" into the design process depends on the overall design philosophy utilized (strength design versus allowable stress design) as discussed in the following section.

During the design process a Perma-Column would be analyzed as three separate components: a reinforced concrete base, a steel attaching bracket, and a steel-to-wood post connection system. Because each of these three elements involves a different combination of materials, three different design specifications actually apply. Specifically, American Concrete Institute (ACI) specifications control the design on the reinforced concrete base, both ACI and American Institute of Steel Construction (AISC) apply to the steel bracket design, and American Wood and Paper Association (AWPA) specifications apply to the steel-to-wood post connection system.

### 2.1 Design Philosophies: Strength Design vs. Allowable Stress Design

Two fundamentally different design procedures are available to determine if a structural component is strong enough to withstand the loads to which it will be subjected: allowable stress design and strength design. As previously mentioned, these two design philosophies primarily differ in how they account for uncertainties in design. In other words, they differ in how they include a factor of safety in structural calculations.

From a safety perspective, it is important to understand that many uncertainties surround structural design. For example, in practice the magnitude of extreme loads may vary from predicted values and simplifying assumptions made during structural analyses may be highly inaccurate.
Additionally, the same analyses may have ignored complex and/or critical interactions between components/systems as well as critical loads and/or load combinations to which the structure is subjected. Also, actual material strengths and dimensions of components used in construction may differ measurably from those assumed during design, and construction oversights may have resulted in critical components being omitted and/or incorrectly installed.

In allowable stress design (ASD), stresses induced in members by nominal (a.k.a. unfactored) loads must not exceed published allowable stresses for the component in question. Safety is accounted for by publishing allowable stress values that are a fraction of the stresses that would result in a failure of the component. In strength design, nominal loads are increased by load factors, and the forces induced in structural components by these factored loads can not exceed published ultimate component strengths that have been reduced by resistance factors. It follows that safety in strength design is accounted for in the load factors and in the resistance factors. To this end, strength design is also referred to as load and resistance factor design (LRFD).

Up until the later 1950's, all wood, steel, and reinforced concrete components were designed using ASD. Traditionally, this design philosophy was referred to as working stress design by the American Concrete Institute (ACI). During the late 1950's, ACI introduced the strength design method as an alternative to their working stress design. During the 1980's, the steel industry followed the concrete industry and developed a strength design methodology which was referred to as LRFD for steel construction. The wood industry followed suit, developing an LRFD or strength design procedure for wood construction in the mid 1990s. However, unlike the concrete and steel industries, the wood industry has been relatively slow to embrace LRFD; that is, the size of virtually all wood members is still determined used ASD procedures.

### 2.2 Governing Equations

The three main equations for strength design can be written as:

$$
\begin{align*}
& \boldsymbol{P}_{u} \leq \phi \boldsymbol{P}_{\boldsymbol{n}}  \tag{2.2.1}\\
& M_{u} \leq \phi \boldsymbol{M}_{\boldsymbol{n}}  \tag{2.2.2}\\
& V_{u} \leq \phi V_{n} \tag{2.2.3}
\end{align*}
$$

where:

| $\boldsymbol{P}_{\boldsymbol{u}}$ | $=$ | Required axial force (axial force due to factored loads) |
| :--- | :--- | :--- |
| $\boldsymbol{M}_{\boldsymbol{u}}$ | $=$ | Required bending moment (bending moment due to factored loads) |
| $\boldsymbol{V}_{\boldsymbol{u}}$ | $=$ | Required shear force (shear force due to factored loads) |
| $\boldsymbol{P}_{\boldsymbol{n}}$ | $=$ | Nominal axial strength |
| $\boldsymbol{M}_{n}$ | $=$ | Nominal moment strength |
| $\boldsymbol{V}_{\boldsymbol{n}}$ | $=$ | Nominal shear strength |
| $\boldsymbol{\phi}$ | $=$ | Resistance factor |
| $\boldsymbol{\phi} \boldsymbol{P}_{\boldsymbol{n}}$ | $=$ | Design (or useable) axial strength |
| $\boldsymbol{\phi} \boldsymbol{M}_{\boldsymbol{n}}$ | $=$ | Design (or useable) moment strength |
| $\boldsymbol{\phi} \boldsymbol{V}_{\boldsymbol{n}}$ | $=$ | Design (or useable) shear strength |

Strength design is recommended when checking the adequacy of the reinforced concrete section and steel attachment bracket of a Perma-Column. Note that in order to do this, design strength values $\boldsymbol{\phi} \boldsymbol{P}_{\boldsymbol{n}}, \boldsymbol{\phi} \boldsymbol{M}_{\boldsymbol{n}}$, and $\boldsymbol{\phi} \boldsymbol{V}_{\boldsymbol{n}}$ must be established for the reinforced concrete section and the steel attachment bracket of each Perma-Column series. This is done in Sections 3 and 4, respectively.

### 2.2 Load Combinations and Load Factors

The resistance factors used in strength design depend on and/or dictate the load factors and corresponding load combinations used during structural analysis to obtain the required strength values (e.g., $\boldsymbol{V}_{\boldsymbol{u}}, \boldsymbol{M}_{\boldsymbol{u}}, \boldsymbol{P}_{\boldsymbol{u}}$ ). To use the resistance factors outlined in following sections for strength design will require use of the following ANSI/ASCE 7 load combinations.

$$
\begin{array}{ll}
1.4 \cdot(\boldsymbol{D}+\boldsymbol{F}) & (2.2 .1) \\
1.2 \cdot(\boldsymbol{D}+\boldsymbol{F}+\boldsymbol{T})+1.6 \cdot(\boldsymbol{L}+\boldsymbol{H})+0.5 \cdot\left(\boldsymbol{L}_{\boldsymbol{r}} \text { or } \boldsymbol{S} \text { or } \boldsymbol{R}\right) \\
1.2 \cdot \boldsymbol{D}+1.6 \cdot\left(\boldsymbol{L}_{\boldsymbol{r}} \text { or } \boldsymbol{S} \text { or } \boldsymbol{R}\right)+(\mathrm{x} \cdot \boldsymbol{L} \text { or } 0.8 \cdot \boldsymbol{W}) \\
1.2 \cdot \boldsymbol{D}+1.6 \cdot \boldsymbol{W}+\mathrm{x} \cdot \boldsymbol{L}+0.5 \cdot\left(\boldsymbol{L}_{r} \text { or } \boldsymbol{S} \text { or } \boldsymbol{R}\right) \\
1.2 \cdot \boldsymbol{D}+1.0 \cdot \boldsymbol{E}+\mathrm{x} \cdot \boldsymbol{L}+0.2 \cdot \boldsymbol{S} \\
0.9 \cdot \boldsymbol{D}+(1.0 \cdot \boldsymbol{E} \text { or } 1.6 \cdot \boldsymbol{W})+1.6 \boldsymbol{H}  \tag{2.2.6}\\
\boldsymbol{D}=\text { Dead Load } \\
\boldsymbol{E}=\text { Earthquake Load } \\
\boldsymbol{F}=\text { Fluid Load } \\
\boldsymbol{H}=\text { Soil Load } \\
\boldsymbol{L}=\text { Live Load } \\
\boldsymbol{L}_{\boldsymbol{r}}=\text { Roof Live Load } \\
\boldsymbol{R}=\text { Rain Load } \\
\boldsymbol{S}=\text { Snow Load } \\
\boldsymbol{T}=\text { Self-Straining Load } \\
\boldsymbol{W}=\text { Wind Load } \\
\text { x }=1.0 \text { for garages, areas of public occupancy, and values of } \boldsymbol{L} \text { greater than } 100 \mathrm{lbf} / \mathrm{ft}^{2} . \text { When } \\
\quad \boldsymbol{L} \text { is less than or equal to } 100 \mathrm{lbf} / \mathrm{ft}^{2} \text {, set x equal to } 0.5 .
\end{array}
$$

## 3. Strength Properties of the Reinforced Concrete

Perma-Columns can be characterized as reinforced concrete members without lateral steel reinforcement. Lateral reinforcement functions as shear reinforcement when the column is subjected to bending loads, and as tie reinforcement when the column is subjected to axial compressive forces. Tie reinforcement is not a necessity in Perma-Columns because of the relatively low axial forces to which the columns are subjected. Such lateral reinforcement would also increase column size. Note that to meet ACI 318 Section 7.10 requirements for tie reinforcement requires a minimum No. 3 size bar spaced no further apart than least dimension of the column. To wrap a No. 3 bar around longitudinal reinforcement and still meet ACI cover requirements would increase member width and thickness by 0.75 inches.
Design (or useable) strength values for the reinforced concrete portion of Perma-Columns are developed in the following sections. Design values are obtained by multiplying nominal strengths by the resistance factors in Table 3.0. These factors are from ACI 318 Appendix C and are only applicable when used in combination with the ASCE/ANSI 7 load factors and combinations in Section 2.2

Table 3.0 - Resistance Factors for Perma-Column Design

| Application | $\phi$ Value |
| :--- | :---: |
| Flexure, without axial load | 0.80 |
| Flexure, with axial tension | 0.80 |
| Axial compression | 0.55 |
| Flexure with axial compression* | 0.55 to 0.80 |
| Axial tension | 0.80 |
| Shear and torsion | 0.75 |

* For low values of axial compression, $\phi$ may be increased towards the value for flexure, 0.80 , according to equations in ACI 318. See Section 3.2.

A resistance factor of 0.55 is listed in Table 3.0 for axial compression and axial compression with flexure. This value is recommended because Perma-Columns do not contain lateral reinforcement. With spiral reinforcement, an axial compression resistance factor of 0.70 would be used. With tie reinforcement, the axial compression resistance factor would be 0.65 . The selected resistance factor of 0.55 is the ACI 318 resistance factor for plain (i. e., non-reinforced) concrete. Note that if Perma-Columns were only subjected to concentrically applied axial loads, it is quite likely that they would not even need longitudinal reinforcement. This is because an upright compression member whose height does not exceed three times its least lateral dimension, is considered a pedestal under ACI 318 Section 22.8 and does not require steel reinforcement. According to the ACI Commentary (ACI 318 Section R22.8), the 3-to-1 limitation on height to thickness ratio does not apply for portions of pedestals embedded in soil capable of providing lateral restraint (Note: In application, Perma-Columns are unlikely to extend more than three times their thickness above grade).

According to ACI 318 Section 10.2, the strength design of members for flexure and axial loads shall be based on the following assumptions:

1. Member strength is based on satisfying applicable conditions of equilibrium and compatibility of strains.
2. Strain in reinforcement and concrete is directly proportional to the distance from the neutral axis.
3. Maximum usable strain $\varepsilon_{c u}$ at extreme concrete compression fiber is equal to 0.003
4. Stress in reinforcement below specified yield strength $\boldsymbol{f}_{\boldsymbol{y}}$ is equal to $\boldsymbol{E}_{\boldsymbol{s}}$ times the steel strain.
5. Tensile strength of concrete shall be neglected in axial and flexural calculations.
6. The relationship between concrete compressive stress distribution and concrete strain when nominal strength is reached may be taken as an equivalent rectangular stress distribution, wherein a concrete stress intensity of $0.85 \boldsymbol{f}_{\boldsymbol{c}}$ ' is assumed to be uniformly distributed over an equivalent compressive zone bounded by the edges of the cross section and a straight line located parallel to the neutral axis at a distance $\boldsymbol{a}=\beta_{I} \boldsymbol{c}$ from the fiber of maximum compressive strain. The distance $\boldsymbol{c}$ from the fiber of maximum strain to the neutral axis is measured in a direction perpendicular to that axis. The value of $\beta_{l}$ is 0.85 for $f_{c}$ ' values less than or equal to 4000 psi and 0.65 for $\boldsymbol{f}_{\boldsymbol{c}}$ ' values greater than or equal to 8000 psi. Linearly interpolation is used to obtain $\boldsymbol{\beta}_{\boldsymbol{I}}$ for $\boldsymbol{f}_{\boldsymbol{c}}$ ' values between 4000 and 8000 psi .

### 3.1 Bending Strength Under Just Flexural Load (No Axially Applied Loads)

Based on the previous assumptions, the following equations can be written for conditions at failure ( $\varepsilon_{c u}=0.003$ and bottom steel yielding) of a Perma-Column subjected to flexure alone. Variables and designated values for each Perma-Column series are given in Tables 1.1 and 3.1:

$$
\begin{align*}
\varepsilon_{s}(t o p) & =0.003\left(\boldsymbol{d}^{\prime}-\boldsymbol{c}\right) / \boldsymbol{c}  \tag{3.1.1}\\
\boldsymbol{C} & =\boldsymbol{\beta}_{\boldsymbol{l}} \boldsymbol{c} \boldsymbol{b} 0.85 \boldsymbol{f}_{\boldsymbol{c}},  \tag{3.1.2}\\
\boldsymbol{T}_{(t o p)} & =\boldsymbol{A}_{\boldsymbol{s}} \boldsymbol{\boldsymbol { E } _ { \boldsymbol { s } } \boldsymbol { \varepsilon } _ { s ( t o p ) } \quad \text { but no greater than } \boldsymbol { f } _ { \boldsymbol { y } } \boldsymbol { A } _ { \boldsymbol { s } } ,} \begin{aligned}
& \boldsymbol{\prime} \\
& \boldsymbol{T}_{(\text {bottom })}=\boldsymbol{A}_{s} \boldsymbol{f}_{\boldsymbol{y}} \\
& \boldsymbol{C}=\boldsymbol{T}_{(t o p)}+\boldsymbol{T}_{(\text {(bottom })}
\end{aligned} \tag{3.1.3}
\end{align*}
$$

Equation 3.1.1 for strain in the top steel returns a negative value when the top steel is located above the neutral axis (i.e., $\boldsymbol{d}^{\prime} \leq \boldsymbol{c}$ ). When this is the case, $\boldsymbol{T}_{(t o p)}$ will have a negative value in all remaining calculations.
Substituting equation 3.1.1 into equation 3.1.3, and then substituting equations 3.1.2, 3.1.3 and 3.1.4 into equation 3.1.5 yields the following equation;

$$
\begin{equation*}
\beta_{I} c b 0.85 f_{c}^{\prime}=A_{s} \boldsymbol{A}_{s} 0.003\left(d^{\prime}-c\right) / c+A_{s} f_{y} \tag{3.1.6}
\end{equation*}
$$

which can be rewritten as:

$$
\begin{equation*}
\boldsymbol{c}^{2}\left[\beta_{l} \boldsymbol{b} 0.85 \boldsymbol{f}_{\boldsymbol{c}}^{\prime} /\left(\boldsymbol{A}_{\boldsymbol{s}}^{\prime} \boldsymbol{f}_{\boldsymbol{y}}\right)\right]+\boldsymbol{c}\left[\left(0.003 \boldsymbol{E}_{\boldsymbol{s}} / \boldsymbol{f}_{\boldsymbol{y}}\right)-\boldsymbol{A}_{\boldsymbol{s}} / \boldsymbol{A}_{\boldsymbol{s}}{ }^{\prime}\right]-0.003 \boldsymbol{d}^{\prime} \boldsymbol{E}_{\boldsymbol{s}} / \boldsymbol{f}_{\boldsymbol{y}}=0 \tag{3.1.7}
\end{equation*}
$$

With the exception of the distance to the neutral axis $\boldsymbol{c}$, all variables in equations 3.1.6 and 3.1.7 are known. Consequently, $\boldsymbol{c}$ can be determined directly using the quadratic equation. Once this is done, the nominal moment strength $\boldsymbol{M}_{\boldsymbol{n}}$ is calculated using the following equation. Note that $\boldsymbol{M}_{\boldsymbol{n}}=$ $\boldsymbol{M}_{\boldsymbol{o}}$ when the member is subjected to flexure alone.

$$
\begin{equation*}
M_{o}=T_{(b o t t o m)}\left(d-\beta_{l} c / 2\right)+T_{(t o p)}\left(d^{\prime}-\beta_{l} c / 2\right) \tag{3.1.8}
\end{equation*}
$$

or

$$
\begin{equation*}
M_{o}=A_{s} f_{y}\left(d-\beta_{I} c / 2\right)+A_{s}^{\prime} E_{s} 0.003\left(d^{\prime}-c\right)\left(d^{\prime} / c-\beta_{I} / 2\right) \tag{3.1.9}
\end{equation*}
$$

Table 3.1. Perma-Column Flexural Strength Characteristics (Under Flexure Alone)

| Variable | Symbol | Units | PC6300 | PC6400 | PC8300 | PC8400 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Stress Block Depth Factor | $\boldsymbol{\beta}_{\boldsymbol{I}}$ |  | 0.65 | 0.65 | 0.65 | 0.65 |
| Distance to Neutral Axis | $\boldsymbol{c}$ | in. | 1.156 | 1.038 | 1.425 | 1.284 |
| Strain in Top Steel | $\boldsymbol{\varepsilon}_{\text {s(top) }}$ | in./in. | 0.00089 | 0.00133 | 0.00028 | 0.00065 |
| Strain in Bottom Steel | $\boldsymbol{\varepsilon}_{\text {s(bot) }}$ | $\mathrm{in} . / \mathrm{in}$. | 0.00722 | 0.00838 | 0.00828 | 0.01013 |
| Conc. Compressive Force | $\boldsymbol{C}$ | lbf | 34341 | 39471 | 42315 | 48802 |
| Net Force in Bottom Steel | $\boldsymbol{T}_{\text {(botom) }}$ | lbf | 24000 | 24000 | 37200 | 37200 |
| Net Force in Top Steel | $\boldsymbol{T}_{\text {(top) }}$ | lbf | 10341 | 15471 | 5115 | 11602 |
| Nominal Moment Strength <br> (flexure alone) | $\boldsymbol{M}_{\boldsymbol{o}}$ | $\mathrm{lbf}-\mathrm{in}$. | 97200 | 104500 | 197400 | 206800 |
| Design (Useable) Strength <br> (flexure alone)* | $\boldsymbol{\phi} \boldsymbol{M}_{\boldsymbol{o}}$ | $\mathrm{lbf}-\mathrm{in}$. | 77700 | 83600 | 158000 | 165400 |

* $\phi=0.80$

Since in all cases, $\boldsymbol{c}$ is less than $\boldsymbol{d}^{\prime}$, the top steel is not located in the compression region. In other words, all steel is tension steel when the nominal moment strength, $\boldsymbol{M}_{\boldsymbol{o}}$ is reached. Table 3.1 values for strain in the top steel are all less than $0.00207 \mathrm{in} . / \mathrm{in}$., thus indicating that the top steel does not yield before a compressive strain (in the extreme concrete fiber in compression) of 0.003 $\mathrm{in} . / \mathrm{in}$. is reached. If the top steel were within $\beta_{I} c$ of the top of the beam, the area of concrete in compression would have to be reduced by the cross sectional area of top steel $\boldsymbol{A}_{\boldsymbol{s}}$,

### 3.2 Axial Load Strength Under Zero Eccentricity (No Flexural Load)

Under typical installation Perma-Columns would be classified as short columns and the nominal axial strength under zero eccentricity would be calculated as:

$$
\begin{equation*}
\boldsymbol{P}_{\boldsymbol{o}}=0.85 \boldsymbol{f}_{\boldsymbol{c}},\left(\boldsymbol{A}_{g}-\boldsymbol{A}_{s t}\right)+\boldsymbol{f}_{\boldsymbol{y}} \boldsymbol{A}_{s t} \tag{3.2.1}
\end{equation*}
$$

Truly concentrically loaded columns (i.e., columns with zero eccentricity) are nonexistent as eccentricity will occur due to slight changes in end conditions, inaccuracy of manufacture, and variations in steel and concrete properties even when the load is theoretically concentric. To account for this eccentricity, ACI 318 Section 10.3.5 requires that the maximum nominal axial strength $\boldsymbol{P}_{\boldsymbol{n}(\max )}$ not exceed $0.80 \boldsymbol{P}_{\boldsymbol{o}}$ for tied columns and $0.85 \boldsymbol{P}_{\boldsymbol{o}}$ for spiral reinforced columns. Because Perma-Columns do not contain any lateral reinforcement, it is recommended that the maximum nominal axial strength $\boldsymbol{P}_{\boldsymbol{n}(\max )}$ be limited to $0.75 \boldsymbol{P}_{\boldsymbol{o}}$, that is:

$$
\begin{equation*}
\boldsymbol{P}_{\boldsymbol{n}(\max )}=0.75 \boldsymbol{P}_{o}=0.75\left[0.85 \boldsymbol{f}_{\boldsymbol{c}},\left(\boldsymbol{A}_{g}-\boldsymbol{A}_{s t}\right)+\boldsymbol{f}_{\boldsymbol{y}} \boldsymbol{A}_{s t}\right] \tag{3.2.2}
\end{equation*}
$$

The $0.75 \boldsymbol{P}_{\boldsymbol{o}}$ limit on $\boldsymbol{P}_{\boldsymbol{n}(\max )}$ is equivalent to an eccentricity of $0.120 \boldsymbol{h}$ for a typical $\boldsymbol{P e r m a}$ -
Column. A $0.80 \boldsymbol{P}_{\boldsymbol{o}}$ limit on $\boldsymbol{P}_{\boldsymbol{n}(\boldsymbol{m a x})}$ would be equivalent to an eccentricity of around $0.093 \boldsymbol{h}$ for a typical Perma-Column. As a rule of thumb, it is good to assume an eccentricity of at least $0.1 \boldsymbol{h}$ when designing columns similar in size to Perma-Columns.
$\boldsymbol{P}_{\boldsymbol{n}(\max )}$ values for Perma-columns, as calculated using equation 3.2.2 are tabulated in Table 3.2

Table 3.2. Perma Column Axial Strength Characteristics (Under Pure Axial Loads)

| Variable | Symbol | Units | PC6300 | PC6400 | PC8300 | PC8400 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total Steel Area | $A_{\text {st }}$ | sq inch | 0.80 | 0.80 | 1.24 | 1.24 |
| Gross Cross-Section Area | $A_{g}$ | sq inch | 29.23 | 37.41 | 38.63 | 49.45 |
| Steel Yield Strength | $\boldsymbol{f}_{\boldsymbol{y}}$ | $\mathrm{lbf} / \mathrm{in} .{ }^{2}$ | 60000 | 60000 | 60000 | 60000 |
| Concrete Comp. Strength | $f_{c}{ }^{\prime}$ | $\mathrm{lbf} / \mathrm{in} .^{2}$ | 10000 | 10000 | 10000 | 10000 |
| Nominal Axial Load Strength at Zero Eccentricity | $P_{\text {o }}$ | Lbf | 289600 | 359200 | 392200 | 484200 |
| Maximum Nominal Axial Load Strength | $\boldsymbol{P}_{\boldsymbol{n} \text { (max) }}$ | Lbf | 217200 | 269400 | 294200 | 363100 |
| Maximum Design (Useable) Axial Load Strength* | $\phi \boldsymbol{P}_{\boldsymbol{n}(\max )}$ | Lbf | 119500 | 148200 | 161800 | 199700 |

* $\phi=0.55$


### 3.3. Strength Under Combined Bending \& Axial Compressive Loads

Seldom, if ever, will a Perma-Column be subjected to a pure axial or a pure bending load. Consequently, allowable axial load/bending moment interactions outlined in this section will typically apply.
The addition of an axial compressive load to a reinforced concrete component that is under a pure bending load will, up to a certain point, increase the amount of bending load to which the concrete member can be subjected (see Figure 3.3.1). This is not the case with a wood, steel, or plain concrete member. This phenomenon results from the fact that the bending strength of a reinforced concrete component under a pure bending load is limited by yielding of tension steel, and the addition of a compressive load: (1) reduces the tensile strain in the tension steel, and (2) increases the area of concrete in compression.


Figure 3.3.1. Strength interaction diagrams for axial compression and bending moment about the major axis of Perma-Columns.
The dots on the diagram in Figure 3.3.1 represent the balanced strain condition $\left(\boldsymbol{P}_{\boldsymbol{n}}=\boldsymbol{P}_{\boldsymbol{b}}, \boldsymbol{M}_{\boldsymbol{n}}=\boldsymbol{M}_{\boldsymbol{b}}\right)$ which is the point at which the tension steel just begins to yield when the maximum concrete strain just reaches 0.003 . There is only one combination of $\boldsymbol{P}_{\boldsymbol{b}}$ and $\boldsymbol{M}_{\boldsymbol{b}}$ under which these two strain states can simultaneously exist. They can be calculated using the following equations.

$$
\begin{align*}
\boldsymbol{c} & =0.003 \boldsymbol{d} /\left(\boldsymbol{f}_{\boldsymbol{y}} / \boldsymbol{E}_{s}+0.003\right)  \tag{3.3.1}\\
\varepsilon_{s(t o p)} & =0.003\left(\boldsymbol{d}^{\prime}-\boldsymbol{c}\right) / \boldsymbol{c}  \tag{3.3.1}\\
\boldsymbol{C} & =\boldsymbol{\beta}_{\boldsymbol{l}} \boldsymbol{c} \boldsymbol{b} 0.85 \boldsymbol{f}_{\boldsymbol{c}},  \tag{3.3.2}\\
\boldsymbol{T}_{(t o p)} & =\boldsymbol{A}_{s}, \boldsymbol{E}_{\boldsymbol{s}} \varepsilon_{s}(t o p) \quad \text { but no greater than } \boldsymbol{f}_{\boldsymbol{y}} \boldsymbol{A}_{s},  \tag{3.3.3}\\
\boldsymbol{T}_{(\text {(botom })} & =\boldsymbol{A}_{s} \boldsymbol{f}_{\boldsymbol{y}}  \tag{3.3.4}\\
\boldsymbol{P}_{\boldsymbol{b}} & =\boldsymbol{C}-\boldsymbol{T}_{(t o p)}-\boldsymbol{T}_{(\text {bottom })}  \tag{3.3.5}\\
\boldsymbol{M}_{b} & =\boldsymbol{C}\left(\boldsymbol{h}-\boldsymbol{\beta}_{l} \boldsymbol{c}\right) / 2-\boldsymbol{T}_{(t o p)}\left(\boldsymbol{h} / 2-\boldsymbol{d}^{\prime}\right)+\boldsymbol{T}_{(\text {bottom })}(\boldsymbol{d}-\boldsymbol{h} / 2) \tag{3.3.6}
\end{align*}
$$

$\boldsymbol{M}_{\boldsymbol{b}}$ and $\boldsymbol{P}_{\boldsymbol{b}}$ are the moment and axial force that produce the same internal affects as $\boldsymbol{C}, \boldsymbol{T}_{\text {(top) }}$, and $\boldsymbol{T}_{(\text {bottom })}$. When calculating $\boldsymbol{M}_{\boldsymbol{b}}$, axial force $\boldsymbol{P}_{\boldsymbol{b}}$ is placed at the plastic centroid of the column. Because of their symmetry, the plastic centroid of Perma-Columns is at the geometric center of the members (i.e., at $\boldsymbol{h} / 2$ ).

All other points that make up the plots in Figure 3.3.1 were obtained in a fashion similar to that use to determine $\boldsymbol{M}_{\boldsymbol{b}}$ and $\boldsymbol{P}_{\boldsymbol{b}}$. Specifically, a strain value was selected for the bottom steel, and the maximum strain in the concrete was fixed at 0.003 . From these two values, the location of the neutral axis and strain in the top steel were calculated. Forces $\boldsymbol{C}, \boldsymbol{T}_{(t o p)}, \boldsymbol{T}_{(b o t t o m)}$ were then calculated and substituted in equations 3.3.5 and 3.3.6 to obtain $\boldsymbol{P}_{\boldsymbol{n}}$ and $\boldsymbol{M}_{\boldsymbol{n}}$, respectively A few of these $\boldsymbol{P}_{\boldsymbol{n}}-\boldsymbol{M}_{\boldsymbol{n}}$ interaction values have been compiled in Table 3.3.1. Radial lines extending from the origin in Figure 3.3.1 represent constant ratios of $\boldsymbol{M}_{\boldsymbol{n}}$ to $\boldsymbol{P}_{\boldsymbol{n}}$, that is they represent eccentricities $\boldsymbol{e}$ of
the load $\boldsymbol{P}_{\boldsymbol{n}}$ from the plastic centroid of the columns. It follows, as shown in figure 3.3.1, that the vertical axis represent $\boldsymbol{e}=0$ and the horizontal axis represents $\boldsymbol{e}=\infty$.

Table 3.3.1 Axial Compression and Bending Strength Interaction Values

| Nominal Axial | Nominal Bending Strength, $\boldsymbol{M}_{\boldsymbol{n}}$, kips-inches |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Strength, $\boldsymbol{P}_{\boldsymbol{n}}$, kips | PC6300 | PC6400 | PC8300 | PC8400 |
| 0 | 97.2 | 104.4 | 197.5 | 206.8 |
| 20 | 127.9 | 136.2 | 243.1 | 253.6 |
| 40 | 157.2 | 167.3 | 287.3 | 299.5 |
| 60 | 175.3 | 196.3 | 324.4 | 343.6 |
| 80 | 181.0 | 214.1 | 360.7 | 380.6 |
| 100 | 186.0 | 221.7 | 370.0 | 417.4 |
| 120 | 189.3 | 228.5 | 371.6 | 439.9 |
| 140 | 189.8 | 233.7 | 372.8 | 444.4 |
| 160 | 186.4 | 236.6 | 372.7 | 448.5 |
| 180 | 177.1 | 236.4 | 369.7 | 451.6 |
| 200 | 160.9 | 232.5 | 361.3 | 453.2 |
| 220 | 131.4 | 223.5 | 349.2 | 452.3 |
| 240 | 101.1 | 208.6 | 332.7 | 446.4 |
| 260 | 63.3 | 188.3 | 311.0 | 437.2 |
| 280 | 17.8 | 155.6 | 283.6 | 424.3 |
| 300 |  | 123.3 | 250.0 | 407.2 |
| 320 | 85.1 | 194.7 | 385.5 |  |
| 340 |  | 40.7 | 146.5 | 359.0 |
| 360 |  |  | 91.2 | 327.3 |
| 380 |  |  | 28.9 | 288.4 |
| 400 |  |  | 232.2 |  |
| 440 |  |  | 128.2 |  |
| 480 |  |  | 9.1 |  |

Design strength values are compiled in Table 3.3.2 and graphically displayed in Figure 3.3.2. These values were obtained by reducing nominal strength values in Table 3.3.1 by appropriate resistance factors. While a resistance factor of 0.80 is applicable to all bending values, the axial resistance factor of 0.55 can be increased to 0.80 (i.e., the resistance factor for bending) as $\boldsymbol{\phi} \boldsymbol{P}_{\boldsymbol{n}}$ decreases from $0.1 \boldsymbol{f}_{\boldsymbol{c}} \boldsymbol{A}_{\boldsymbol{g}}$ to zero.
To check the adequacy of a design, first divide the moment due to factored load $\boldsymbol{M}_{\boldsymbol{u}}$, by the compression axial force due to factored load, $\boldsymbol{P}_{\boldsymbol{u}}$, to obtain the eccentricity due to factored loads. Next, find the eccentricity (in the far right column of Table 3.3.2) and associated $\boldsymbol{\phi}_{a} \boldsymbol{P}_{\boldsymbol{n}}$ and $\boldsymbol{\phi}_{b} \mathbf{M}_{\mathbf{n}}$ values that correspond to the calculated eccentricity. The design in question is adequate in compression and bending as long as the $\boldsymbol{\phi}_{a} \boldsymbol{P}_{\boldsymbol{n}}$ value exceeds $\boldsymbol{P}_{u}$ and the $\phi_{b} \boldsymbol{M}_{\boldsymbol{n}}$ value exceeds $\boldsymbol{M}_{u}$.

Table 3.3.2 Axial Compression and Bending Strength Design Values

| Notable Points | $\begin{gathered} \boldsymbol{P}_{\boldsymbol{n}} \\ \text { kips } \\ \hline \end{gathered}$ | $\phi_{a}$ | $\begin{aligned} & \boldsymbol{\phi}_{\boldsymbol{a}} \boldsymbol{P}_{\boldsymbol{n}} \\ & \text { kips } \\ & \hline \end{aligned}$ | $\begin{gathered} \boldsymbol{M}_{\boldsymbol{n}} \\ \text { kips-inch } \\ \hline \end{gathered}$ | $\begin{gathered} \phi_{b} \mathbf{M}_{\mathbf{n}} \\ \text { kips-inches } \\ \hline \end{gathered}$ | Eccentricity, $\boldsymbol{e}$, inches |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PC6300 |  |  |  |  |  |  |
| $\begin{array}{r} \phi_{a} P_{n}=0.1 f_{c}^{\prime} A_{g} \rightarrow \\ \text { Balanced Condition } \rightarrow \end{array}$ | 0.0 | 0.80 | 0.0 | 97.2 | 77.8 | $\infty$ |
|  | 20.0 | 0.71 | 14.1 | 127.9 | 102.3 | 7.25 |
|  | 40.0 | 0.61 | 24.5 | 157.2 | 125.8 | 5.14 |
|  | 53.1 | 0.55 | 29.2 | 172.1 | 137.7 | 4.71 |
|  | 54.5 | 0.55 | 30.0 | 173.6 | 138.9 | 4.64 |
|  | 60.0 | 0.55 | 33.0 | 175.3 | 140.3 | 4.25 |
|  | 80.0 | 0.55 | 44.0 | 181.0 | 144.8 | 3.29 |
|  | 100.0 | 0.55 | 55.0 | 186.0 | 148.8 | 2.71 |
|  | 120.0 | 0.55 | 66.0 | 189.3 | 151.4 | 2.29 |
|  | 140.0 | 0.55 | 77.0 | 189.8 | 151.8 | 1.97 |
|  | 160.0 | 0.55 | 88.0 | 186.4 | 149.1 | 1.69 |
|  | 180.0 | 0.55 | 99.0 | 177.1 | 141.7 | 1.43 |
|  | 200.0 | 0.55 | 110.0 | 160.9 | 128.7 | 1.17 |
| Max. Axial Strength $\boldsymbol{\rightarrow}$ | 217.2 | 0.55 | 119.5 | 135.5 | 108.4 | 0.91 |
| PC6400 |  |  |  |  |  |  |
| $\begin{array}{r} \phi_{a} P_{n}=0.1 f_{c}^{\prime} A_{g} \rightarrow \\ \text { Balanced Condition } \rightarrow \end{array}$ | 0.0 | 0.80 | 0.0 | 104.4 | 83.6 | $\infty$ |
|  | 20.0 | 0.73 | 14.5 | 136.2 | 108.9 | 7.50 |
|  | 40.0 | 0.65 | 26.1 | 167.3 | 133.8 | 5.12 |
|  | 60.0 | 0.58 | 34.8 | 196.3 | 157.0 | 4.52 |
|  | 68.0 | 0.55 | 37.4 | 205.1 | 164.1 | 4.39 |
|  | 73.8 | 0.55 | 40.6 | 211.5 | 169.2 | 4.17 |
|  | 80.0 | 0.55 | 44.0 | 214.1 | 171.3 | 3.89 |
|  | 100.0 | 0.55 | 55.0 | 221.7 | 177.3 | 3.22 |
|  | 120.0 | 0.55 | 66.0 | 228.5 | 182.8 | 2.77 |
|  | 140.0 | 0.55 | 77.0 | 233.7 | 187.0 | 2.43 |
|  | 160.0 | 0.55 | 88.0 | 236.6 | 189.3 | 2.15 |
|  | 180.0 | 0.55 | 99.0 | 236.4 | 189.2 | 1.91 |
|  | 200.0 | 0.55 | 110.0 | 232.5 | 186.0 | 1.69 |
|  | 220.0 | 0.55 | 121.0 | 223.5 | 178.8 | 1.48 |
|  | 240.0 | 0.55 | 132.0 | 208.6 | 166.9 | 1.26 |
|  | 260.0 | 0.55 | 143.0 | 188.3 | 150.7 | 1.05 |
| Max. Axial Strength $\rightarrow$ | 269.4 | 0.55 | 148.2 | 173.0 | 138.4 | 0.93 |

Table 3.3.2 Axial Compression and Bending Strength Design Values, cont.

| Notable Points | $\begin{gathered} \hline \boldsymbol{P}_{\boldsymbol{n}} \\ \text { kips } \\ \hline \end{gathered}$ | $\phi_{a}$ | $\begin{aligned} & \boldsymbol{\phi}_{\boldsymbol{a}} \boldsymbol{P}_{\boldsymbol{n}} \\ & \text { kips } \\ & \hline \end{aligned}$ | $\begin{gathered} \hline \boldsymbol{M}_{\boldsymbol{n}} \\ \text { kips-inch } \\ \hline \end{gathered}$ | $\begin{gathered} \hline \phi_{b} \mathbf{M}_{\mathbf{n}} \\ \text { kips-inches } \\ \hline \end{gathered}$ | Eccentricity, $\boldsymbol{e}$, inches |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PC8300 |  |  |  |  |  |  |
| $\phi_{a} P_{n}=0.1 f_{c}, A_{g} \rightarrow$ | 0.0 | 0.80 | 0.0 | 197.5 | 158.0 |  |
|  | 20.0 | 0.73 | 14.6 | 243.1 | 194.5 | 13.34 |
|  | 40.0 | 0.66 | 26.3 | 287.3 | 229.8 | 8.74 |
|  | 60.0 | 0.59 | 35.2 | 324.4 | 259.5 | 7.37 |
|  | 70.2 | 0.55 | 38.6 | 342.9 | 274.4 | 7.10 |
|  | 80.0 | 0.55 | 44.0 | 360.7 | 288.5 | 6.56 |
| Balanced Condition $\rightarrow$ | 85.3 | 0.55 | 46.9 | 368.5 | 294.8 | 6.29 |
|  | 100.0 | 0.55 | 55.0 | 370.0 | 296.0 | 5.38 |
|  | 120.0 | 0.55 | 66.0 | 371.6 | 297.3 | 4.50 |
|  | 140.0 | 0.55 | 77.0 | 372.8 | 298.2 | 3.87 |
|  | 160.0 | 0.55 | 88.0 | 372.7 | 298.1 | 3.39 |
|  | 180.0 | 0.55 | 99.0 | 369.7 | 295.7 | 2.99 |
|  | 200.0 | 0.55 | 110.0 | 361.3 | 289.0 | 2.63 |
|  | 220.0 | 0.55 | 121.0 | 349.2 | 279.4 | 2.31 |
|  | 240.0 | 0.55 | 132.0 | 332.7 | 266.1 | 2.02 |
|  | 260.0 | 0.55 | 143.0 | 311.0 | 248.8 | 1.74 |
|  | 280.0 | 0.55 | 154.0 | 283.6 | 226.9 | 1.47 |
| Max. Axial Strength $\rightarrow$ | 294.2 | 0.55 | 161.8 | 259.8 | 207.8 | 1.28 |
| PC8400 |  |  |  |  |  |  |
| $\phi_{a} P_{n}=0.1 f_{c}, A_{g} \rightarrow$ | 0.0 | 0.80 | 0.0 | 206.8 | 165.4 |  |
|  | 20.0 | 0.74 | 14.9 | 253.6 | 202.9 | 13.63 |
|  | 40.0 | 0.69 | 27.6 | 299.5 | 239.6 | 8.70 |
|  | 60.0 | 0.63 | 38.0 | 343.6 | 274.9 | 7.24 |
|  | 80.0 | 0.58 | 46.2 | 380.6 | 304.5 | 6.59 |
|  | 89.9 | 0.55 | 49.5 | 398.8 | 319.1 | 6.45 |
|  | 100.0 | 0.55 | 55.0 | 417.4 | 333.9 | 6.07 |
| Balanced Condition $\rightarrow$ | 112.8 | 0.55 | 62.0 | 437.8 | 350.2 | 5.64 |
|  | 120.0 | 0.55 | 66.0 | 439.9 | 351.9 | 5.33 |
|  | 140.0 | 0.55 | 77.0 | 444.4 | 355.5 | 4.62 |
|  | 160.0 | 0.55 | 88.0 | 448.5 | 358.8 | 4.08 |
|  | 180.0 | 0.55 | 99.0 | 451.6 | 361.3 | 3.65 |
|  | 200.0 | 0.55 | 110.0 | 453.2 | 362.6 | 3.30 |
|  | 220.0 | 0.55 | 121.0 | 452.3 | 361.8 | 2.99 |
|  | 240.0 | 0.55 | 132.0 | 446.4 | 357.1 | 2.71 |
|  | 260.0 | 0.55 | 143.0 | 437.2 | 349.8 | 2.45 |
|  | 280.0 | 0.55 | 154.0 | 424.3 | 339.5 | 2.20 |
|  | 300.0 | 0.55 | 165.0 | 407.2 | 325.7 | 1.97 |
|  | 320.0 | 0.55 | 176.0 | 385.5 | 308.4 | 1.75 |
|  | 340.0 | 0.55 | 187.0 | 359.0 | 287.2 | 1.54 |
|  | 360.0 | 0.55 | 198.0 | 327.3 | 261.8 | 1.32 |
| Max. Axial Strength $\rightarrow$ | 363.1 | 0.55 | 199.7 | 321.2 | 256.9 | 1.29 |



Figure 3.3.2. Design bending and axial strength interaction values for Perma-Columns.

### 3.4 Shear Strength

The nominal shear strength of a reinforced concrete component, $\boldsymbol{V}_{\boldsymbol{n}}$, is equal to the sum of the shear strength provided by the concrete, $\boldsymbol{V}_{c}$, and the shear strength provided by shear reinforcement, $\boldsymbol{V}_{\boldsymbol{s}}$, that is, $\boldsymbol{V}_{\boldsymbol{n}}=\boldsymbol{V}_{\boldsymbol{c}}+\boldsymbol{V}_{\boldsymbol{s}}$. Because they do not contain shear reinforcement, $\boldsymbol{V}_{\boldsymbol{n}}=\boldsymbol{V}_{\boldsymbol{c}}$ for a Perma-Column. It should be noted that ACI 318 Section 11.5.5.1 restricts $\boldsymbol{V}_{\boldsymbol{n}}$ to $\boldsymbol{V}_{c} / 2$ for most components that do not contain reinforcement. The increase from $\boldsymbol{V}_{\boldsymbol{n}}=\boldsymbol{V}_{\boldsymbol{c}} / 2$ to $\boldsymbol{V}_{\boldsymbol{n}}=\boldsymbol{V}_{\boldsymbol{c}}$ is allowed for Perma-Columns because their overall depth is less than 10 inches.
For members subjected to shear and flexure only, $\boldsymbol{V}_{\boldsymbol{c}}$ can be taken as the greater of:

$$
\begin{equation*}
V_{c}=2.0 b \boldsymbol{b}\left(f_{c},\right)^{1 / 2} \tag{3.4.1}
\end{equation*}
$$

or

$$
\begin{equation*}
V_{c}=1.9 b d\left(f_{c}\right)^{1 / 2}+2500 A_{s} d V_{u} / M_{u} \tag{3.4.2}
\end{equation*}
$$

but not greater than:

$$
\begin{equation*}
V_{c}=3.5 b d\left(f_{c},\right)^{1 / 2} \tag{3.4.3}
\end{equation*}
$$

or

$$
\begin{equation*}
\boldsymbol{V}_{\boldsymbol{c}}=1.9 \boldsymbol{b} \boldsymbol{d}\left(f_{\boldsymbol{c}},\right)^{1 / 2}+2500 \boldsymbol{A}_{\boldsymbol{s}} \tag{3.4.4}
\end{equation*}
$$

Where $\left(\boldsymbol{f}_{\boldsymbol{c}}\right)^{1 / 2}$ shall not be taken to be greater than $100 \mathrm{lbf} / \mathrm{in}^{2}$. Note that equation 3.4.4 limits the ratio of $\boldsymbol{d} \boldsymbol{V}_{\boldsymbol{u}} / \boldsymbol{M}_{\boldsymbol{u}}$ in equation 3.4.2 to unity. Perma-Column design shear strength values ( $\phi \boldsymbol{V}_{\boldsymbol{n}}$ ) calculated using equations 3.4.1 through 3.4.4 are compiled in Table 3.4.1. Note that in all cases, equation 3.3.4 and not equation 3.4.3 controls the maximum design shear strength.

## Table 3.4.1 Shear Strength Design Values

(Without Increases From Axial Compressive Forces)

|  | PC6300 |  | PC6400 |  | PC8300 |  | PC8400 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} V_{n}=V_{c} \\ \mathrm{lbf} \\ \hline \end{gathered}$ | $\begin{gathered} \phi V_{n}{ }^{*} \\ \mathrm{lbf} \\ \hline \end{gathered}$ | $\begin{gathered} V_{n}=V_{c} \\ \text { lbf } \end{gathered}$ | $\begin{gathered} \phi V_{n}{ }^{*} \\ \mathrm{lbf} \\ \hline \end{gathered}$ | $\begin{gathered} V_{n}=V_{c} \\ \text { lbf } \end{gathered}$ | $\begin{gathered} \phi V_{n}{ }^{*} \\ \mathrm{lbf} \\ \hline \end{gathered}$ | $\begin{gathered} V_{n}=V_{c} \\ \mathrm{lbf} \\ \hline \end{gathered}$ | $\begin{gathered} \phi V_{\boldsymbol{n}}{ }^{*} \\ \mathrm{lbf} \\ \hline \end{gathered}$ |
| Minimum from Equation 3.4.1 | 4236 | 3177 | 5421 | 4066 | 6042 | 4531 | 7733 | 5800 |
| Maximum from Equation 3.4.4 | 5024 | 3768 | 6150 | 4613 | 7289 | 5467 | 8896 | 6672 |
| $M_{u} / V_{u}$, in. |  |  |  |  |  |  |  |  |
| $\cdots$ | 5009 | 3757 | 6135 | 4602 | 7917 | 5938 | 9524 | 7143 |
| $\stackrel{+}{\sim}$ | 4812 | 3609 | 5938 | 4454 | 7482 | 5611 | 9089 | 6816 |
| \% 6 | 4680 | 3510 | 5807 | 4355 | 7191 | 5393 | 8798 | 6599 |
| - 8 | 4516 | 3387 | 5643 | 4232 | 6828 | 5121 | 8435 | 6327 |
| 采 10 | 4418 | 3313 | 5544 | 4158 | 6611 | 4958 | 8218 | 6163 |
| 以 12 | 4352 | 3264 | 5479 | 4109 | 6465 | 4849 | 8072 | 6054 |
| 14 | 4305 | 3229 | 5432 | 4074 | 6362 | 4771 | 7969 | 5977 |
| 16 | 4270 | 3202 | ** | ** | 6284 | 4713 | 7891 | 5918 |
|  | ** | ** | ** | ** | 6175 | 4631 | 7782 | 5837 |
| $>\quad 24$ | ** | ** | ** | ** | 6102 | 4577 | ** | ** |
| 28 | ** | ** | ** | ** | 6051 | 4538 | ** | ** |

* $\phi=0.75$ for shear
** Minimum value from equation 3.4.1 is greater

Although the design shear strength of a component $\phi V_{n}$ decreases as the ratio of bending moment to shear load induced by the factored loads $\left(\boldsymbol{M}_{u} / V_{u}\right)$ increases, any axial compressive load induced by the factored loads will increase design shear strength. To this end, ACI allows use of the following equations for members subjected to axial compression in addition to bending:

$$
\begin{equation*}
\boldsymbol{V}_{\boldsymbol{c}}=1.9 \mathrm{~b} \boldsymbol{d}\left(\boldsymbol{f}_{\boldsymbol{c}}\right)^{1 / 2}+2500 \boldsymbol{A}_{\boldsymbol{s}} \boldsymbol{d} \boldsymbol{V}_{\boldsymbol{u}} /\left\{\boldsymbol{M}_{\boldsymbol{u}}-\boldsymbol{N}_{\boldsymbol{u}}(4 \boldsymbol{h}-\boldsymbol{d}) / 8\right\} \tag{3.4.5}
\end{equation*}
$$

However, $\boldsymbol{V}_{c}$ can not be greater than:

$$
\begin{equation*}
V_{c}=3.5 \mathrm{~b} d\left(f_{c}\right)^{1 / 2}\left\{1+\boldsymbol{N}_{u} /\left(500 A_{g}\right)\right\}^{1 / 2} \tag{3.4.6}
\end{equation*}
$$

Where $N_{u}$ is the axial force in lbf due to factored loads (positive for compression and negative for tension). When the quantity $\left\{\boldsymbol{M}_{\boldsymbol{u}}-\boldsymbol{N}_{\boldsymbol{u}}(4 \boldsymbol{h}-\boldsymbol{d}) / 8\right\}$ in equation 3.4.5 is negative, $\boldsymbol{V}_{\boldsymbol{c}}$ shall be calculated using equation 3.4.6.

Since $\boldsymbol{N}_{\boldsymbol{u}}$ cannot exceed $\boldsymbol{\phi}_{\boldsymbol{a}} \boldsymbol{P}_{\boldsymbol{n}}$, the maximum $\boldsymbol{N}_{\boldsymbol{u}}$ values for PC6300, PC6400, PC8300 and PC8400 are $119.5,148.2,161.8$ and 199.7 kips, respectively (see Table 3.3.2). Substituting these values into equation 3.4.6 and multiplying by a resistance factor of 0.75 produces the following maximums for $\phi V_{\boldsymbol{n}}=\boldsymbol{\phi} \boldsymbol{V}_{\boldsymbol{c}}: 168.4,212.5,242.8$ and 305.8 kips for PC6300, PC6400, PC8300 and PC8400, respectively.

Design shear strengths $\phi \boldsymbol{V}_{\boldsymbol{n}}$ for PC6300 columns, obtained by multiplying $\boldsymbol{V}_{\boldsymbol{c}}$ values from Equation 3.4.5 by a shear resistance factor of 0.75 , are shown in Figure 3.4.1 for a variety of $M_{u} / V_{u}$ and $N_{u} / V_{u}$ combinations.


Figure 3.4.1. Design shear strengths $\phi V_{n}$ for PC6300 columns as a function of $M_{u} / V_{u}$ and $N_{u} / V_{u}$

### 3.5 Comparison With Wood Strength Values

A common question is how do Perma-Column design strength values compare with those of the laminated wood posts they replace or to which they are attached? Prior to making some of these comparisons, the following points should be understood.

1. Wood strengths are dependent upon the duration of the applied load. The amount of load a wood component can sustain decreases the longer the load acts upon the structure. There is no time dependent reduction in the amount of load a reinforced concrete component can sustain.
2. Magnitude of bending moment applicable to a reinforced concrete component increases as axial compressive load is applied to the component. Conversely, the magnitude of bending moment that can be applied to a wood member decreases as an axial compressive load is applied to the component.
3. The magnitude of shear force to which a reinforced concrete component can be subjected increases as an axial compressive load is applied to the component, but decreases as the bending moment in the member increases. The design shear strength of a wood member is not measurably affected by the axial or bending forces acting on the member.
4. Wood design values must be reduced when wood is used in a moist environment. After initial curing, concrete design strengths are not affected by changes in the moisture content of the surrounding environment.
Table 3.5.1 contains load and resistance factor design (LRFD) values for mechanically-laminated posts fabricated from No. 1 Southern Yellow Pine and used where the wood moisture content will exceed $19 \%$ for extended time periods. No. 1 Southern Yellow Pine is a common visual grade for laminated posts. Note that any post that would be used in place of a Perma-Column would have to be designed for higher moisture contents. Also, like the concrete design strengths established in previous sections, the LRFD values for wood in Table 3.5.1 must be used in conjunction with the load combinations and load factors in Section 2.2.

Figure 3.5.1 contains a graphical comparison of maximum allowed axial and bending moment induced by wind loads for Perma-Columns and No. 1 Southern Yellow Pine posts. Values for the Perma-Columns are the same as those shown in Figure 3.3.2. Note that the axes have been retitled with $\boldsymbol{\phi} \boldsymbol{P}_{\boldsymbol{n}}$ replaced by $\boldsymbol{P}_{\boldsymbol{u}}$ (i.e., $\boldsymbol{P}_{\boldsymbol{u}} \leq \boldsymbol{\phi} \boldsymbol{P}_{\boldsymbol{n}}$ ) and $\boldsymbol{\phi} \boldsymbol{M}_{\boldsymbol{n}}$ replaced by $\boldsymbol{M}_{\boldsymbol{u}}$. The relationships between $\boldsymbol{P}_{\boldsymbol{u}}$ and $\boldsymbol{M}_{\boldsymbol{u}}$ for the wood posts were calculated using the following design equation for wood members under combined bending and axial compressive loads.

$$
\begin{equation*}
\left[\frac{\boldsymbol{P}_{u}}{\lambda \phi_{c} \boldsymbol{P}^{\boldsymbol{\prime}}}\right]^{2}+\frac{\boldsymbol{M}_{\boldsymbol{m}}}{\lambda \phi_{b} \boldsymbol{M}^{\boldsymbol{\prime}}} \leq 1.0 \tag{3.5.1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\boldsymbol{P}_{\boldsymbol{u}} & =\text { Axial compressive force due to factored loads } \\
\lambda \boldsymbol{\phi}_{\boldsymbol{c}} \boldsymbol{P} & =\text { Design resistance for axial compression from Table 3.5.1 } \\
\boldsymbol{M}_{\boldsymbol{m}} & =\text { Factored moment, including any magnification for second-order effects } \\
& =\boldsymbol{M}_{\boldsymbol{u}} \text { for short columns } \\
\boldsymbol{\lambda \phi _ { \boldsymbol { b } } \boldsymbol { M } ^ { \prime }} & =\text { Adjusted moment resistance from Table 3.5.1 }
\end{aligned}
$$

Table 3.5.1 Properties of Mechanically-Laminated No. 1 Southern Yellow Pine Columns*

| Variable Description | Symbol | Unit |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Physical Characteristics |  |  |  |  |  |  |
| Number of Plys |  |  | 3 | 4 | 3 | 4 |
| Nominal Ply Size |  | in. $x$ in. | 2 x 6 | 2 x 6 | 2 x 8 | 2 x 8 |
| Cross-Sectional Area | A | in. ${ }^{2}$ | 24.75 | 33.00 | 32.63 | 43.50 |
| Section Modulus | $S$ | in. ${ }^{3}$ | 22.69 | 30.25 | 39.42 | 52.56 |
| Tabulated Reference Strength Values |  |  |  |  |  |  |
| Shear | $\boldsymbol{F}_{v}$ | kips/in. ${ }^{2}$ | 0.26 | 0.26 | 0.26 | 0.26 |
| Flexure | $\boldsymbol{F}_{\boldsymbol{b}}$ | kips/in. ${ }^{2}$ | 4.19 | 4.19 | 3.81 | 3.81 |
| Axial Compression | $F_{\text {c }}$ | kips/in. ${ }^{2}$ | 4.20 | 4.20 | 3.96 | 3.96 |

## Applicable Adjustment Factors

| Wet Service Factor - Shear | $C_{M}$ |  | 0.97 | 0.97 | 0.97 | 0.97 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Wet Service Factor - Flexure | $C_{M}$ |  | 0.85 | 0.85 | 0.85 | 0.85 |
| Wet Service Factor - Axial Comp. | $C_{M}$ |  | 0.80 | 0.80 | 0.80 | 0.80 |
| Shear Stress Factor** | $\boldsymbol{C}_{\boldsymbol{H}}$ |  | 1.95 | 1.95 | 1.95 | 1.95 |
| Load Sharing Factor*** | $C_{r}$ |  | 1.35 | 1.35 | 1.40 | 1.40 |
| Adjusted Reference Strength Values |  |  |  |  |  |  |
| Shear ( $\boldsymbol{F}_{\boldsymbol{v}} \boldsymbol{C}_{\boldsymbol{M}} \boldsymbol{C}_{\boldsymbol{H}}$ ) | $F_{v}{ }^{\prime}$ | kips/in. ${ }^{2}$ | 0.49 | 0.49 | 0.49 | 0.49 |
| Flexure ( $\boldsymbol{F}_{\boldsymbol{b}} \boldsymbol{C}_{\boldsymbol{M}} \boldsymbol{C}_{\boldsymbol{r}}$ ) | $F_{b}{ }^{\text {, }}$ | kips/in. ${ }^{2}$ | 4.81 | 4.81 | 4.53 | 4.53 |
| Axial Compression ( $\boldsymbol{F}_{\boldsymbol{b}} \boldsymbol{C}_{\boldsymbol{M}}$ ) | $F_{c}{ }^{\prime}$ | kips/in. ${ }^{2}$ | 3.36 | 3.36 | 3.17 | 3.17 |
| Adjusted Resistance Values |  |  |  |  |  |  |
| Shear ( $\left.\boldsymbol{F}_{\boldsymbol{v}}{ }^{\prime} \boldsymbol{A} / 1.5\right)$ | $V^{\prime}$ | kips | 8.11 | 10.82 | 10.70 | 14.26 |
| Moment ( $\boldsymbol{F}_{\boldsymbol{b}} \boldsymbol{S} \boldsymbol{S}$ ) | M' | kips-in. | 109.1 | 145.4 | 178.7 | 238.3 |
| Axial Compression ( $\left.\boldsymbol{F}_{\boldsymbol{c}}^{\prime} \boldsymbol{A}\right)$ | $P$ ' | kips | 83.2 | 110.9 | 103.4 | 137.8 |

Resistance and Time Effect Factors

| Resistance Factor - Shear | $\phi_{v}$ | 0.75 | 0.75 | 0.75 | 0.75 |
| ---: | :---: | :---: | :---: | :---: | :---: |
| Resistance Factor - Bending | $\phi_{b}$ | 0.85 | 0.85 | 0.85 | 0.85 |
| Resistance Factor - Axial Comp. | $\phi_{c}$ | 0.90 | 0.90 | 0.90 | 0.90 |
| Time Effect Factor - Wind Load | $\lambda_{w}$ | 1.0 | 1.0 | 1.0 | 1.0 |
| Time Effect Factor - Snow Load | $\lambda_{s}$ | 0.8 | 0.8 | 0.8 | 0.8 |


| Design Resistance Values Under Wind Loading |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shear | $\lambda_{w} \phi_{v} V^{\prime}$ | kips | 6.09 | 8.11 | 8.02 | 10.70 |
| Moment | $\lambda_{w} \phi_{b} M^{\prime}$ | kips-in. | 92.7 | 123.6 | 151.9 | 202.6 |
| Axial Compression | $\lambda_{w} \phi_{c} P^{\prime}$ | kips | 74.8 | 99.8 | 93.0 | 124.0 |
| Design Resistance Values Under Snow Loading |  |  |  |  |  |  |
| Shear | $\lambda_{s} \phi_{v} V^{\prime}$ | kips | 4.87 | 6.49 | 6.42 | 8.56 |
| Moment | $\lambda_{s} \phi_{b} M^{\prime}$ | kips-in. | 74.2 | 98.9 | 121.5 | 162.1 |
| Axial Compression | $\lambda_{s} \phi_{c} \boldsymbol{P}^{\prime}$ | kips | 59.9 | 79.8 | 74.4 | 99.2 |

[^1]

Figure 3.5.1. Interaction diagrams for maximum allowed axial and bending moment induced by wind loads for Perma-Columns and No. 1 Southern Yellow Pine posts.

Table 3.5.2 Comparison of Perma-Column and Wood Post Shear Strengths

| Variable Description | Units | 3-ply <br> 2x6 | 4-ply <br> 2x6 | 3-ply <br> $\mathbf{2 x 8}$ | 4-ply <br> $\mathbf{2 x 8}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| LRFD Design Shear Strength for No.1 SP <br> (Wind Load) | kips | 6.09 | 8.11 | 8.02 | 10.70 |
| ACI Design Shear Strength (No Bending) | kips | 3.77 | 4.61 | 5.47 | 6.67 |
| Average Maximum Test Shear | kips | 10.55 | 11.08 | 16.36 | 19.02 |
| Average Maximum Test Shear x 0.55 | kips | 5.80 | 6.09 | 9.00 | 10.46 |

Table 3.5.2 contains Perma-Column and No. 1 Southern Yellow Pine design shear strength values. As evidenced from the table, the American Forest \& Paper Association (AF\&PA) LRFD values for the wood posts exceed the ACI design shear values for the Perma-Columns by an average $55 \%$. However, as evidenced from actual bending test data (Appendix C), the Perma-Column design shear values are extremely conservative. When a conservative resistance factor of 0.55 is applied to the Perma-Column test values, there is essentially no difference between the design shear strengths of the No. 1 SP posts and the Perma-Columns.

## 4. Strength Properties of the Steel Bracket

Using published procedures to determine design values for Perma-Column components is a straight forward process with two exceptions, that being the determination of design values for the shear and bending strength of the steel bracket-to-concrete connection. Because of the complex geometry and interaction between steel and concrete at the steel bracket-to-concrete connection, neither ACI or AISC (American Institute of Steel Construction) design procedures can be applied. To this end, engineers are required to rely on laboratory tests that have been specially designed to isolate the shear strength and bending strength of the joint.

### 4.1 Bending Strength

Bending strength of the steel bracket, or more specifically, the steel bracket-to-concrete connection, was determined by laboratory testing. Test procedures, equipment and results are presented in Appendix B along with a brief discussion.

Translating test values to design strengths requires (1) a selection of a nominal bending strength, $\boldsymbol{M}_{\boldsymbol{n}}$, and (2) application of a resistance factor for bending $\phi_{b}$. Selection of a nominal bending strength is complicated issue that requires additional investigation. Because of the ductility of the connection, one may want to assign a limit state of 0.02 or 0.03 radians to the connection. Nominal bending strength would then be the bending strength associated with the selected rotation. This is not an uncommon approach for steel connections characterized by larger deformations. With a nominal bending strength so defined, a bending resistance factor of 0.90 would be appropriate.

### 4.2 Shear Strength

All shear related failures associated with the shear tests described in Appendix C occurred on "non-bracketed" ends of test specimens. This means that the shear strength of a steel bracket-toconcrete connection is at least as great as that for the reinforced concrete base. This is not surprising since the steel bracket functions much like shear reinforcing in that it ties longitudinal reinforcing together. Consequently, as long as the reinforced concrete portion of a PermaColumn is shown to adequately handle applied shear forces, there is no need to check the shear capacity of the steel bracket-to-concrete column connection.

## 5. Stiffness of the Reinforced Concrete

Calculation of a structural component's bending deflections requires knowledge of the flexural rigidity of the component. For components manufactured from a single, homogenous material (e.g. steel) and possessing a constant cross-section, flexural rigidity is simply equal to the product of the modulus of elasticity of the material and the moment of inertia associated with the component's cross-section.

Calculation of the flexural rigidity of a reinforced concrete component is not as straight forward as that for most wood or steel components for two primary reasons. First, a reinforced concrete member consists of two materials (concrete and steel) each with a different modulus of elasticity. Second, the cross-sectional moment of inertia of a reinforced concrete component changes rapidly once a tension crack forms in the concrete. Because tension cracking is directly related to the applied bending moment, and applied bending moment generally varies significantly along a component, cracking (and hence effective moment of inertia) will vary along the length of the component.
To simplify flexural rigidity calculations for reinforced concrete components, the component is treated as a solid "non-reinforced" concrete component. For cracked cross-sections, this requires transformation of the cross-sectional area of reinforcing steel to an equivalent cross-sectional area of concrete. When reinforced concrete components are treated as solid concrete components, the modulus of elasticity assigned to the member is the modulus of elasticity for the concrete.

### 5.1 Concrete Modulus of Elasticity

ACI 8.5.1 states that the modulus of elasticity for concrete, $\boldsymbol{E}_{\boldsymbol{c}}$, for normal weight concrete shall be calculated as $57,000\left(\boldsymbol{f}_{\boldsymbol{c}}\right)^{0.5}$ where $\boldsymbol{f}_{\boldsymbol{c}}$, is the specified concrete strength in $\mathrm{lbf} / \mathrm{in}^{2}$. Given an $\boldsymbol{f}_{\boldsymbol{c}}$ ' of $10,000 \mathrm{lbf} / \mathrm{in}^{2}$ this equates to a $\boldsymbol{E}_{\boldsymbol{c}}$ for Perma-Columns of 5,700,000 lbf $/ \mathrm{in}^{2}$.

### 5.2 Reinforced Concrete Moment of Inertia

ACI 9.5.2.3 states that immediate deflections shall be calculated using $\boldsymbol{E}_{\boldsymbol{c}}$ and an effective moment of inertia, $\boldsymbol{I}_{e}$, that is calculated using the following formula, but is not greater than $\boldsymbol{I}_{\boldsymbol{g}}$.

$$
\begin{equation*}
\boldsymbol{I}_{e}=\left(\boldsymbol{M}_{c r} / \boldsymbol{M}_{a}\right)^{3} \boldsymbol{I}_{g}+\left[1-\left(\boldsymbol{M}_{c r} / \boldsymbol{M}_{a}\right)^{3}\right] \boldsymbol{I}_{c r} \tag{5.2.1}
\end{equation*}
$$

where:

$$
\begin{aligned}
\boldsymbol{I}_{e} & =\text { Effective moment of inertia for deflection calculations, in }{ }^{4} \\
\boldsymbol{I}_{\boldsymbol{c} r} & =\text { Moment of inertia of cracked section transformed to concrete, in } \\
\boldsymbol{I}_{\boldsymbol{g}} & =\text { Moment of inertia of gross concrete section about centroidal axis, neglecting } \\
& \text { reinforcement, in }^{4} \\
\boldsymbol{M}_{\boldsymbol{a}} & =\text { Maximum moment in member at stage deflection is computed, in-lbf } \\
\boldsymbol{M}_{c r} & =\text { Cracking moment, in-lbf } \\
& =\boldsymbol{f}_{\boldsymbol{r}} \boldsymbol{I}_{g} / \boldsymbol{y}_{t} \\
\boldsymbol{f}_{\boldsymbol{r}} & =\text { Modulus of rupture of concrete, lbf/in }{ }^{2} \\
& =7.5\left(\boldsymbol{f}_{\boldsymbol{c}},{ }^{0}\right)^{0.5} \text { for normal weight concrete } \\
& =750 \mathrm{lbf} / \mathrm{in}^{2} \text { for Perma-Columns } \\
\boldsymbol{y}_{t} & =\text { Distance from centroidal axis of gross section neglecting reinforcement, to extreme } \\
& \text { fiber in tension, inches }
\end{aligned}
$$

Effective moment of inertia values calculated using equation 5.2.1 are compiled in Table 5.1 and have been plotted in Figure 5.2.1.

Table 5.2.1: Perma Column Moment of Inertia Values



Figure 5.2.1. Effective moment of inertia for strong axis bending of Perma-Columns as a function of actual bending moment.

Although the actual bending moment (and hence effective moment of inertia) varies along the length of a member, Equation 5.2.1 assumes that the effective moment of inertia used in modeling will be fixed for the entire length (i.e., span) of the member. The specific $\boldsymbol{I}_{e}$ to use for such modeling should be that calculated using Equation 5.2 .1 with $\boldsymbol{M}_{a}$, set equal to the maximum actual bending moment for the entire span. ACI 9.5.2.4 recommends using the bending moment located at the midspan of simple and continuous spans, and the bending moment located at the support for cantilevers.

Equation 5.2.1 is based on the work of Dan E. Branson ("Instantaneous and Time-Dependent Deflections of Simple and Continuous Reinforced Beams," Part 1, Report No. 7 Alabama Highway Research Report, Bureau of Public Roads, August 1963). For engineers wishing to recognize the continuous variation of the moment of inertia with span, Branson proposed using the fourth power instead of the third power in Equation 5.2.1. In this case, $\boldsymbol{M}_{\boldsymbol{c}}$ and $\boldsymbol{M}_{\boldsymbol{a}}$ would be the cracking and applied moment, respectively, at each segment along the span.

## 6. Rotational Stiffness of Steel Bracket-to-Wood Connection

The moment-rotational relationship (a.k.a. rotational stiffness) of the steel bracket-to-wood connection can be estimated once the shear load-slip relationship (a.k.a. the slip modulus) of the individual fasteners has been established and the geometry of the fastener pattern has been specified.

### 6.1 Fastener Slip Modulus

The slip modulus of a fastener is the ratio of (1) the shear load transferred by the fastener, and (2) the slip between the two components being connected by the fastener (a.k.a. interlayer slip). While the relationship between fastener shear load and interlayer slip is non-linear (especially near ultimate load), it is sufficiently linear at lower loads to justify use of a fixed value for most structural analyses.

Based on Perma-Column steel bracket-to-wood connection testing reported in Appendix D, a slip modulus of $85,500 \mathrm{lbf} / \mathrm{inch}$ is recommended for a 0.5 -inch diameter SAE grade 5 bolt in double shear. Similarly, a slip modulus of $28,700 \mathrm{lbf} / \mathrm{inch}$ is recommended for a 0.25 -inch diameter Simpson Strong-Drive ${ }^{\circledR}$ wood screw in single shear. These values should be relatively accurate for any steel bracket-to-wood connection featuring lumber with a specific gravity near 0.50 .


Figure 6.1.1. Rotation between wood post and steel bracket under a pure bending moment when two identical fastener groups are spaced a distance, $s$.

Figure 6.1.1 illustrates the rotation between a Perma-Column steel bracket and post under a pure bending moment, $\boldsymbol{M}$. Each of the small boxes in Figure 6.1.1 represents an individual fastener or a small group of closely spaced fasteners. When there is a small group of fasteners, it is advantageous to assign a slip modulus to the entire group. This is simply accomplished by summing the slip modulus values of the individual fasteners comprising the group. For example, if the group contains one 0.5 -inch diameter bolt in double shear and two SDS screws in single shear, the slip modulus for the group would equal 85,500 plus $2 \times 287,000$ or $142,900 \mathrm{lbf} / \mathrm{inch}$.

### 6.2. Rotational Stiffness

The rotational stiffness of a connection is the ratio of applied moment, $\boldsymbol{M}$, to rotation, $\boldsymbol{\theta}$, as defined in Figure 6.1.1. To obtain a relationship between $\boldsymbol{M}$ and $\boldsymbol{\theta}$, use is made of the fact that the distance from the center of joint rotation to a fastener or fastener group, $s / 2$, when multiplied by rotation, $\boldsymbol{\theta}$, is equal to the interlayer slip of the fastener or fastener group, $\boldsymbol{\Delta}$. Interlayer slip is in turn equal to the shear force applied to the fastener or fastener group, $\boldsymbol{F}$, divided by the slip modulus, $\boldsymbol{k}$. Finally, shear force, $\boldsymbol{F}$, when multiplied by the fastener spacing, s, is equal to the applied bending moment, $\boldsymbol{M}$. In equation form

$$
\begin{align*}
& \boldsymbol{\Delta}=\boldsymbol{\theta} \boldsymbol{s} / 2  \tag{6.2.1}\\
& \boldsymbol{k}=\boldsymbol{F} / \boldsymbol{\Delta}  \tag{6.2.2}\\
& \boldsymbol{M}=\boldsymbol{F} \boldsymbol{s} \tag{6.2.3}
\end{align*}
$$

From these equations the following relationship for rotation stiffness can be obtained.

$$
\begin{equation*}
M / \theta=k s^{2} / 2 \tag{6.2.4}
\end{equation*}
$$

Where:
$\boldsymbol{M}=$ Applied bending moment
$\boldsymbol{\theta}=$ Joint rotation
$\boldsymbol{k}=$ Slip modulus for a fastener or fastener group
$\boldsymbol{s}=$ Spacing between fasteners or fastener groups

### 6.3 Connection Modeling

Adequate assessment of the impact of joint behavior on structural load distribution requires proper modeling of the moment-rotational relationship. This a very straight forward process when the structural analysis program incorporates special joint elements that enable designers to simply enter the rotational stiffness as calculated using equation 6.2.4.

When special joint elements are not available, a designer can model the joint using a simple beam or frame element. The flexural rigidity, $\boldsymbol{E I}$, that must be assigned to this element is given as:

$$
\begin{equation*}
\boldsymbol{E} \boldsymbol{I}=\boldsymbol{k} \boldsymbol{s}^{2} \boldsymbol{L}_{\mathrm{e}} / 2 \tag{6.3.1}
\end{equation*}
$$

Where:
$\boldsymbol{E I}=$ Product of the modulus of elasticity and moment of inertia assigned to the modeling

$\boldsymbol{k}=$ element
$\boldsymbol{s}=$ Slip modulus for a fastener or fastener group
$\boldsymbol{L}_{\mathrm{e}}=$ Length of the modeling element

Output from the structural analyses will include the bending moment, $\boldsymbol{M}$. By dividing this bending moment by the spacing between the fastener groups, $\boldsymbol{s}$, the force $\boldsymbol{F}$ on each group is obtained. If there is more than one fastener in the group, it is important to realize that this force $\boldsymbol{F}$ is divided among the individual fasteners in accordance with their individual slip modulus. In equation form:

$$
\begin{align*}
F_{i} & =M \boldsymbol{k}_{i} /(\boldsymbol{s} \boldsymbol{k})  \tag{6.3.2}\\
\boldsymbol{F}_{i} & =\boldsymbol{F} \boldsymbol{k}_{i} / \boldsymbol{k} \tag{6.3.3}
\end{align*}
$$

Where:
$\boldsymbol{F}_{\boldsymbol{i}}=$ Shear force on fastener $\boldsymbol{i}$ where $\boldsymbol{i}$ is one fastener within a group of fasteners
$\boldsymbol{F}=$ Total shear force acting on fastener group
$\boldsymbol{k}_{\boldsymbol{i}}=$ Slip modulus of fastener $\boldsymbol{i}$
$\boldsymbol{k}=$ Slip modulus for fastener group

## Appendix A: Column Bending Tests

## A. 1 Introduction, Test Methods and Equipment

Several Perma-Columns where loaded to failure in bending to validate ACI design values. These Perma-Columns were supported and loaded as shown in Figure A.1. The spacing of 48 inches between supports was selected to provide sufficient bearing at supports while also providing a shear span to effective beam depth ratio that would push the bending strength limits of the columns during test. In this particular case, the shear span is equal to 24 inches - the distance between a support and the load point. With an effective depth of 3.97 inches, the shear span to depth ratio ( $a / d$ ratio) for PC6300 and PC6400 series columns is 6.04 . The effective depth of 5.53 inches for PC8300 and PC8400 columns results in an $a / d$ ratio of 4.34 .


Figure A.1. Bending test set-up for Perma-Columns.

Beams with an $a / d$ ratio greater than 6 fall under the general category of long beams. Beams with an $a / d$ ratio between about 2.5 and 6 fall under the general category of intermediate length beams. Long beams typically fail in flexure. Failure begins with yielding of the tension reinforcement and ends by crushing of the concrete at the point of maximum bending moment. In addition to nearly vertical flexural cracks near the point of maximum bending moment, prior to failure slightly inclined cracks may be present between the support and region of maximum bending moment (Wang and Salmon, 1985). For intermediate length beams, vertical cracks form first, followed by inclined flexure-shear cracks. At the sudden occurrence of a flexure-shear crack, a beam is not able to redistribute load and additional load can generally not be sustained. The load corresponding to the point at which the flexure-shear crack forms represents the shear strength of the beam (Wang and Salmon, 1985).

Columns were loaded using a Tinius Olson Universal Compression-Tension Testing Machine. Load-head rate was fixed at 0.2 inches/minute. Applied load and load-head movement were recorded at 0.5 second intervals using a Campbell Scientific CR23X datalogger.

## A. 2 Results

Table A. 1 contains the load-head displacement, maximum applied load, maximum shear load (i.e., $1 / 2$ total applied load) and corresponding maximum bending moment at the point of maximum load for each test specimen. Figure A. 2 contains a plot of midspan displacement versus shear/bending moment for each Perma-Column series. Data for each curve in this figure was obtained by averaging load-displacement data for all specimens tested of that particular series.

Table A. 1 Perma-Column Bending Test Results

| PermaColumn <br> Series | Replicate Number | Load-Head Disp. at Max. Load, inches | Maximum Applied Load, kips | Maximum Shear Force, kips | Max. Bending Moment, inch-kips |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PC6300 | 1 | 0.71 | 10.5 | 5.23 | 125.5 |
|  | 3 | 0.73 | 10.4 | 5.19 | 124.7 |
|  | 4 | 0.65 | 10.5 | 5.26 | 126.2 |
|  | 5 | * | 10.6 | 5.31 | 127.5 |
|  | 6 | 0.68 | 10.8 | 5.39 | 129.2 |
|  | Average | 0.69 | 10.6 | 5.28 | 126.6 |
|  | COV** | 5.0 \% | 1.4 \% | 1.4 \% | 1.4 \% |
| PC6400 | 1 | 0.71 | 10.8 | 5.42 | 130.1 |
|  | 2 | 0.78 | 10.6 | 5.29 | 126.9 |
|  | 3 | * | 11.6 | 5.78 | 138.7 |
|  | 4 | 0.83 | 10.5 | 5.23 | 125.4 |
|  | 5 | 0.88 | 12.0 | 5.98 | 143.4 |
|  | Average | 0.80 | 11.1 | 5.54 | 132.9 |
|  | COV** | 9.1\% | 5.9 \% | 5.9 \% | 5.9 \% |
| PC8300 | 1 | 0.41 | 17.4 | 8.71 | 209.1 |
|  | 2 | 0.38 | 15.7 | 7.85 | 188.5 |
|  | 3 | 0.36 | 16.0 | 7.98 | 191.4 |
|  | Average | 0.38 | 16.4 | 8.18 | 196.4 |
|  | COV** | 6.6 \% | 5.7 \% | 5.7 \% | 5.7 \% |
| PC8400 | 1 | 0.42 | 19.7 | 9.86 | 236.6 |
|  | 2 | 0.32 | 18.6 | 9.32 | 223.6 |
|  | 3 | 0.35 | 18.1 | 9.03 | 216.6 |
|  | 4 | 0.44 | 19.7 | 9.84 | 236.1 |
|  | Average | 0.38 | 19.0 | 9.51 | 228.2 |
|  | COV** | 14.8 \% | 4.3 \% | 4.3 \% | 4.3 \% |

* Not recorded
** Coefficient of Variation $=$ Standard Deviation x 100 /Average
Perma-Columns failed as expected given their $a / d$ ratios. With their long beam classification in this test, PC6300 and PC6400 series columns were expected to exhibit a pure bending failure and did. A typical PC6300/PC6400 failure, which is shown in Figure A.3, was characterized by formation of vertical tension cracks, followed by tension steel yielding and eventual concrete crushing at midspan. A typical PC8300/PC8400 failure is shown in Figure A.4. Unlike their shallower counterparts, failure of these columns was controlled by their shear strength as is evidenced by the flexure-shear crack in Figure A.4.

The difference in failure modes between PC6300/PC6400 series columns and PC8300/PC8400 series columns is reflected in the load-displacement plots in Figure A.2. Curves associated with bending failures are smooth as tension steel continues to yield. Failures associated with shear are abrupt as flexure-shear cracks suddenly form. The slight difference between PC6300 and PC6400 at low loads in attributable to the greater width, and hence greater uncracked moment of inertia of the PC6400 series. At high loads there is no difference between PC6300 and PC6400 columns as
their behavior near failure is due to the relative location and cross-sectional area of tension steel which is identical in both series. In the case of PC8300 and PC8400 columns, concrete crosssectional area (which is greater in PC8400) controls strength and stiffness right up to failure.


Figure A.2. Average load-head displacement versus shear force/midspan bending moment.


Figure A.3. Bending failure mode characteristic of all PC6300 and PC6400 series columns.


Figure A.4. Shear failure mode characteristic of all PC8300 and PC8400 series columns.

## A. 3 Comparisons

Table A. 2 compares bending test results with ACI nominal shear and bending moment strength values ( $\boldsymbol{V}_{\boldsymbol{n}}$ and $\boldsymbol{M}_{\boldsymbol{n}}$ values, respectively).
Table A. 2 Comparison of Test Results With ACI Nominal Strengths

| Perma- <br> Column <br> Series | Property | Average Test <br> Maximum | ACI <br> Nominal <br> Strength | Ratio, <br> Test/ACI | Test <br> Underestimates <br> Maximum <br> Strength? |
| :--- | :--- | :---: | :---: | :---: | :---: |
| PC6300 | Shear, kips | 5.28 | $4.24^{*}$ | 1.25 | Yes |
|  | Bending Moment, inch-kips | 126.6 | 97.2 | 1.30 | No |
| PC6400 | Shear, kips | 5.54 | $5.42^{*}$ | 1.02 | Yes |
|  | Bending Moment, inch-kips | 132.9 | 104.5 | 1.27 | No |
| PC8300 | Shear, kips | 8.18 | $6.10^{*}$ | 1.34 | No |
|  | Bending Moment, inch-kips | 196.4 | 197.4 | 1.00 | Yes |
| PC8400 | Shear, kips | 9.51 | $7.73^{*}$ | 1.23 | No |
|  | Bending Moment, inch-kips | 228.2 | 206.8 | 1.10 | Yes |

* From Table 3.4.1 $M_{u} / V_{u}=24$ inches

In all cases, actual assembly strength surpassed ACI nominal values, even in those cases where the average test maximum was not associated with the cause of failure. For example, tests of PC8300 and PC8400 columns ended when the shear capacity of the assemblies was reached; consequently,
the associated bending moments listed in Tables A. 1 and A. 2 are less than the actual bending capacity of the assemblies.

It is clearly evident from Table A. 2 that ACI nominal shear strengths underestimate the actual shear strength of the assemblies by at least $20 \%$. This can be partly attributed to the quality of the concrete used in the manufacture of Perma-Columns.

## A. 4 References

Wang and Salmon. 1985. Reinforced Concrete Design. $4^{\text {th }}$ Edition. Harper \& Row Publishers. New York, New York.

## Appendix B: Bracket Bending Tests

## B. 1 Test Methods and Equipment

Several Perma-Columns where loaded to failure in bending to determine the flexural strength and stiffness of the steel bracket-to-concrete column connection. The $1 / 3$ point loading arrangement shown in Figures B. 1 and B. 2 was used with the interface between the steel bracket and the concrete located in the center of the shear-free, constant-moment region (i.e., the region between the two load points).

3 in.


Figure B.1. Bending test set-up for Perma-Column steel bracket-to-concrete column connection.


Figure B.2. Bending test set-up for Perma-Column steel bracket-to-concrete column connection showing LVDT used to measure joint rotation.

Loads were applied using a Tinius Olson Universal Compression-Tension Testing Machine as shown in Figure B.2. Load-head rate was fixed at 0.6 inches/minute. A linear variable differential transformer (LVDT) attached as shown in Figure B. 2 was used to measure bending rotation between the concrete column and steel bracket. The core of the LVDT was placed on the edge of the bracket at a location 12 inches from concrete-to-steel bracket interface. Applied load, loadhead movement, and displacements measured with the LVDT were recorded at 0.5 second intervals using a Campbell Scientific CR23X datalogger.

Six specimens each of Series PC6300 and PC8400, and four specimens each of PC6400 and PC8300 were tested. Replicates 5 and 6 of PC8400 where fabricated with \#4 rebar instead of the standard \#5 rebar used in these assemblies.

## B. 2 Results

Table B. 1 contains the maximum applied load and corresponding load-head displacement, end shear (i.e., $1 / 2$ total applied load) and bending moment for each test specimen.
Table B. 1 Perma-Column Bracket Bending Test Results

|  | PC6300 |  | PC6400 |  | PC8300 |  | PC8400* |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rep. | Max. | Load | Head | Max. | Load | Head | Max. | Load |
|  | Head | Max. | Load |  |  |  |  |  |
|  | Load | Disp. | Load | Disp. | Load | Disp. | Load | Disp. |
|  | kips | inches | kips | inches | kips | inches | kips | inches |
| 1 | 5.26 | 4.27 | 5.44 | 4.64 | 8.74 | 3.20 | 10.94 | 4.46 |
| 2 | 4.83 | 3.61 | 5.28 | 4.35 | 8.37 | 2.65 | 10.61 | 4.33 |
| 3 | 4.76 | 3.42 | 5.57 | 5.17 | 9.41 | 4.05 | 7.94 | 2.79 |
| 4 | 4.56 | 3.12 | 5.53 | 4.06 | 8.84 | 4.36 | 7.40 | 2.68 |
| 5 | 5.10 | 3.86 |  |  |  |  | 8.79 |  |
| 6 | 5.04 | 3.89 |  |  |  |  | 8.38 | 3.85 |
|  | Max. | Max. | Max. | Max. | Max. | Max. | Max. | Max. |
| Rep. | End | Bending | End | Bending | End | Bending | End | Bending |
|  | Shear | Moment | Shear | Moment | Shear | Moment | Shear | Moment |
|  | kips | in.-kips | kips | in.-kips | kips | in.-kips | kips | in.-kips |
| 1 | 2.63 | 99.8 | 2.72 | 103.3 | 4.37 | 166.1 | 5.47 | 207.9 |
| 2 | 2.42 | 91.8 | 2.64 | 100.4 | 4.18 | 158.9 | 5.31 | 201.6 |
| 3 | 2.38 | 90.5 | 2.79 | 105.9 | 4.71 | 178.8 | 3.97 | 150.9 |
| 4 | 2.28 | 86.6 | 2.77 | 105.1 | 4.42 | 168.0 | 3.70 | 140.7 |
| 5 | 2.55 | 97.0 |  |  |  |  | 4.40 | 167.0 |
| 6 | 2.52 | 95.8 |  |  |  |  | 4.19 | 159.3 |
| Average | 2.46 | 93.58 | 2.73 | 103.66 | 4.42 | 167.96 | 4.51 | 171.22 |
| Std Dev | 0.127 | 4.844 | 0.064 | 2.436 | 0.217 | 8.228 | 0.723 | 27.468 |
| COV | 0.052 | 0.052 | 0.024 | 0.024 | 0.049 | 0.049 | 0.160 | 0.160 |
| $5 \%$ E.L.** |  | 85.6 |  | 99.6 |  | 154.4 |  | 126.0 |

[^2]The LVDT was used to measure rotation of the steel bracket-to-concrete connection because previous testing showed this to be a major component of total bending deformation. In this study, load head displacement provides a relative measure of column bending deformation. That said, it should be noted that load head displacement, as recorded in this study, was not just due to flexure of the column assembly, but also included a relatively small amount of deformation associated with strain in assembly supports, load blocks and the load distributing beam.

That portion of the total load head displacement that is directly attributable to deformation (i.e., rotation) of the steel bracket-to-concrete connection was obtained by dividing connection rotation (in radians) by two and multiplying by 38 inches (i.e., the distance between a support and adjacent load point). A comparison of this displacement with total load head displacement is graphically illustrated for each Perma-Column series in Figure B.3.


Figure B.3. Relative portion of total load-head displacement due to rotation of the steel bracket-to-concrete column connection.

Figure B. 4 contains a plot of midspan bending moment versus connection rotation for each of the columns series. Data used to generate these plots is compiled in Table B.2. These values represent the average of data from the various specimen tests. It is important to note that there was essentially no difference between load-displacement curves of individual replications of a particular column series. Likewise, there was little difference between the moment-rotation curves of replicates of a particular column series.


Figure B.4. Joint rotation versus bending moment for steel bracket-to-concrete connection. Plotted from data compiled in Table B.2.

Table B.2. Joint Rotation Vs. Bending Moment for Steel Bracket-to-Concrete Connections

| PC6300 |  | PC6400 |  | PC8300 |  | PC8400 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rotation | Moment | Rotation | Moment | Rotation | Moment | Rotation | Moment |
| radians | in.-kips | radians | in.-kips | radians | in.-kips | radians | in.-kips |
| 0.00203 | 7.0 | 0.00233 | 8.1 | 0.00185 | 12.9 | 0.00198 | 12.2 |
| 0.00465 | 15.0 | 0.00508 | 17.2 | 0.00400 | 28.9 | 0.00446 | 28.5 |
| 0.00700 | 20.9 | 0.00780 | 23.8 | 0.00610 | 39.6 | 0.00694 | 42.0 |
| 0.00900 | 25.7 | 0.01025 | 29.9 | 0.00810 | 48.7 | 0.00916 | 54.1 |
| 0.01115 | 30.3 | 0.01278 | 35.3 | 0.01043 | 57.7 | 0.01184 | 64.7 |
| 0.01320 | 35.0 | 0.01550 | 40.5 | 0.01295 | 67.1 | 0.01420 | 74.0 |
| 0.01540 | 39.4 | 0.01850 | 45.0 | 0.01573 | 75.6 | 0.01712 | 83.5 |
| 0.01778 | 43.9 | 0.02153 | 49.6 | 0.01873 | 83.2 | 0.02030 | 92.2 |
| 0.02040 | 48.1 | 0.02478 | 52.8 | 0.02238 | 90.3 | 0.02374 | 99.8 |
| 0.02305 | 51.6 | 0.02833 | 57.2 | 0.02638 | 97.2 | 0.02732 | 107.3 |
| 0.02613 | 55.5 | 0.03195 | 61.1 | 0.03048 | 104.6 | 0.03122 | 113.8 |
| 0.02948 | 58.9 | 0.03590 | 64.7 | 0.03475 | 111.5 | 0.03526 | 119.4 |
| 0.03303 | 62.1 | 0.04015 | 67.9 | 0.03920 | 117.9 | 0.03954 | 125.3 |
| 0.03683 | 65.2 | 0.04470 | 70.9 | 0.04370 | 123.9 | 0.04408 | 130.4 |
| 0.04073 | 67.8 |  |  |  |  | 0.04874 | 135.1 |
| 0.04523 | 70.4 |  |  |  |  | 0.05364 | 138.9 |

PC6300 and PC6400 assemblies failed due to concrete crushing that was preceded by significant yielding of tension side steel (see Figure B.5). While most PC8300 and PC8400 failed in a similar fashion, a couple failed (e.g., PC8400 replicates 3 and 4) when high stress concentrations due to excessive deformation resulted in a fracture of the tension steel-to-steel bracket interface as shown in Figure B.6.


Figure B.5. Typical bending failure mode for steel bracket-to-concrete connection.


Figure B.6. Fracture of tension steel rebar connection in PC8400 replicate 4.

## B. 3 Discussion

Table B. 3 contains a comparison of mean bracket bending strengths to (1) bending strength values for the reinforced concrete sections from test (Appendix A), and (2) calculated ACI nominal bending strength values from Section 3.1. The more realistic comparisons are those for series PC6300 and PC6400 because the failure mode associated with maximum bracket bending strength was the same as that for the reinforced column tests (Appendix A), that is, failure in both cases
resulted from concrete crushing after significant yielding of tension steel. As the footnote in Table B. 3 points out, comparisons of maximum bracket bending strengths for PC8300 and PC8400 with bending strengths from Appendix A are not as meaningful as strengths reported in Appendix A for those series was controlled by shear (and not bending) strength.

Table B.3. Comparison of Bracket Bending Strength to Column Bending Strength Values

| Variable | PC6300 | PC6400 | PC8300 | PC8400 |
| :--- | :---: | :---: | :---: | :---: |
| Mean Bending Strength, inch-kips | 93.6 | 103.7 | 168.0 | 171.2 |
| Ratio of Mean Bending Strength to Reinforced <br> Concrete Bending Strength As Determined By Test | $73.9 \%$ | $78.0 \%$ | $85.5 \%^{*}$ | $75.0 \%^{*}$ |
| Ratio of Mean Bending Strength to ACI Reinforced <br> Concrete Nominal Bending Strength | $96.3 \%$ | $99.2 \%$ | $85.1 \%$ | $82.8 \%$ |

* Percentages inflated because bending strength values from Appendix A for PC8300 and PC8400 are not maximum bending strengths as maximum load was limited by shear strength.


Figure B.7. Relationship between maximum applied load and load-head displacement.

The maximum load values and associated load-head displacements listed in Table B. 1 have been plotted in Figure B.7. This figure shows that higher maximum loads are associated with higher displacements at failure. This is logical since load continues to increase as tension steel yields and displacement increases.

The plots in Figure B. 3 illustrate that deformation in the joint area accounts for an increasing percentage of total load-head displacement as load increases. At approximately $75 \%$ of maximum load, joint rotation accounts for the bulk of the load-head displacement. This is due to the formation of a plastic hinge in the joint region.
The switch from \#5 to a \#4 rebar in replicates 5 and 6 of the PC8400 series appears to have had a significant affect on joint bending strength when these two replicates are compared to PC8400 replicates 1 and 2 which had similar failure modes. This is expected as joint bending strength is directly related to tension steel cross-sectional area.

## Appendix C: Shear Tests

## C. 1 Test Methods and Equipment

Twelve Perma-Columns where loaded to failure to determine the shear strength of the assemblies. The $1 / 3$ point loading arrangement shown in Figure C. 1 was used. Loads were applied using the Tinius Olson Universal Compression-Tension Testing Machine shown in Figure C.2. Load-head rate was fixed at 0.2 inches/minute. Three specimens of each Perma-Column Series were tested.


Figure C.1. Test set-up for determining Perma-Column shear strength.


Figure C.2. Load application with a Tinius Olson Universal Compression-Tension Testing Machine.

The 18 inch distance between beam support and beam load point results in a $a / d$ ratio of 4.6 for the PC6300 and PC6400 Perma-Columns, and a/d ratio of 3.2 for the PC8300 and PC8400 Perma-Columns. As noted in Appendix A, beams with an a/d ratio between about 2.5 and 6 fall under the general category of intermediate length beams. For intermediate length beams, vertical cracks form first, followed by inclined flexure-shear cracks. At the sudden occurrence of a flexure-shear crack, a beam is not able to redistribute load and additional load can generally not be sustained. The load corresponding to the point at which the flexure-shear crack forms represents the shear strength of the beam (Wang and Salmon, 1985).

## C. 2 Results

Table C. 1 contains the maximum end shear (i.e., $1 / 2$ total applied load) and the maximum bending moment for each test specimen.

Table C. 1 Perma-Column Shear Test Results

|  | PC6300 |  | PC6400 |  | PC8300 |  | PC8400 |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rep. | Max. | Max. | Max. | Max. | Max. | Max. | Max. | Max. |  |  |  |  |  |  |
|  | Shear | Bending | Shear | Bending | Shear | Bending | Shear | Bending |  |  |  |  |  |  |
|  | Force | Moment | Force | Moment | Force | Moment | Force | Moment |  |  |  |  |  |  |
|  | kips | in.-kips | kips | in.-kips | kips | in.-kips | kips | in.-kips |  |  |  |  |  |  |
| 1 | 6.14 | 110.5 | 5.86 | 105.6 | 12.58 | 226.4 | 13.74 | 247.3 |  |  |  |  |  |  |
| 2 | 5.65 | 101.8 | $6.43^{*}$ | $115.7^{*}$ | 13.93 | 250.8 | $13.93^{*}$ | $250.7^{*}$ |  |  |  |  |  |  |
| 3 | 6.12 | 110.1 | 6.01 | 108.2 | 12.97 | 233.5 | $13.59^{*}$ | $244.6^{*}$ |  |  |  |  |  |  |
| Average | 5.97 | 107.5 | 6.10 | 109.8 | 13.16 | 236.9 | 13.75 | 247.5 |  |  |  |  |  |  |
| Std Dev | 0.27 | 4.9 | 0.29 | 5.2 | 0.70 | 12.6 | 0.17 | 3.0 |  |  |  |  |  |  |
| COV, \% | 4.59 | 4.78 |  |  |  |  |  |  |  |  | 5.23 |  |  |  |

* Bending related failure at bracket end of specimen

There were two distinctly different failure modes associated with the tests. Nine of the twelve specimens exhibited a shear failure on the "non-bracketed" end of the specimen as shown in the top and middle pictures in Figure C.3. Maximum load in the other three specimens (one PC8300 and two PC8400) was limited by a bending related failure of the steel bracket-to-concrete column connection. This failure mode is shown in the bottom photograph in Figure C.3.

## C. 3 Comparisons

Table C. 2 contains a comparison of test results with ACI nominal strengths. Because this test was structured to determine the shear strength of the assemblies, the tests should not underestimate maximum shear strengths (as was the case with the bending tests reported in Appendix A). However, because of the two bending related failures associated with PC8400 specimens, it could be argued that the test results still underestimate the average maximum shear strength of the PC8400 assemblies. It is for this reason that the word "maybe" appears in the far right column of the Table C.2.

The test-to-ACI shear strength ratios of 2.12 and 1.76 in Table C. 2 demonstrate that the average maximum shear strength values for the PC8300 and PC8400 Series Perma-Columns are significantly greater than the ACI nominal strengths. These ratios are also measurably greater than the test-to-ACI shear strength ratios of 1.34 and 1.23 reported for the same column series in Appendix A.


Figure C.3. Inclined cracking associated with shear failure of PC6300 (top) and PC8300 (middle) specimens. Bending failure at the steel bracket-to-concrete column connection (bottom) in a PC8400 specimen.

Table C. 2 Comparison of Test Results With ACI Nominal Strengths

| Perma- <br> Column <br> Series | Property | Average Test <br> Maximum | ACI <br> Nominal <br> Strength | Ratio, <br> Test/ACI | Test <br> Underestimates <br> Maximum <br> Strength? |
| :--- | :--- | :---: | :---: | :---: | :---: |
| PC6300 | Shear, kips | 5.97 | $4.24^{*}$ | 1.41 | No |
|  | Bending Moment, inch-kips | 107.5 | 97.2 | 1.11 | Yes |

* From Table 3.4.1 $\boldsymbol{M}_{u} / \boldsymbol{V}_{\boldsymbol{u}}=18$ inches

The three bending failures were a direct result of the relatively high loads that the assemblies were able to sustain. Because the shear strengths were higher than originally predicted (based on Appendix A data), bending moments in the vicinity of the steel bracket-to-concrete column connection reached failure levels (see Appendix B) prior to the assembly failing in shear.

## C. 4 Concrete Compressive Strength

Five 3- by 6-inch concrete cylinders that were cast along with the Perma-Column shear tests specimens were tested 28 days after fabrication (Figure C.4). The resulting compressive strengths were $9656,11302,11309,11116$ and 11492 lbf per square inch for an average compressive strength of 10975 psi.


Figure C.4. Compressive strength testing of concrete used in shear test specimens.

## Appendix D: Steel Bracket-to-Wood Connection Tests

## D. 1 Overview

A series of tests were conducted to examine the performance of three different steel bracket-towood connections. These tests were conducted for two primary purposes. First, there was interest in determining the relative strength of (1) connections made with two 0.5 - by 5.0 -inch SAE grade 5 bolts, (2) connections made with twelve 0.25 - by 3.0 -inch Simpson Strong-Drive ${ }^{\circledR}$ wood screws (a.k.a. SDS screws), and (3) connections featuring two 0.5 - by 5.0 -inch bolts and four of the 0.25 inch diameter SDS screws. These three connection types are herein referred to as the bolt, screw, and combo connections, respectively. The second objective of these tests was to determine bending moment-rotation relationships for the connections.

The three different connections were made using the steel bracket design shown in Figure D.1. This bracket was designed so that (1) two identical bent plates could be welded together to form a single bracket, and (2) bolt holes, but not screw holes, would line up after the bent plates were welded together. There were six 0.25 -inch diameter and two 0.50 -inch diameter holes in each plate. The relative arrangement of 0.25 -inch diameter holes $\mathrm{A}, \mathrm{B}$ and C was identical on both ends of the plate. The white dots in Figure D. 1 show the location of holes on the backside of the bracket after two identical bent plates were welded together.


Figure D.1. Dimensions and hole pattern for steel bracket used in connection tests.
The four SDS screws used in the "combo" connection tests were located in holes labeled with an "A" in Figure D.1.

## D. 2 Wood Properties

Wood properties can significantly affect the strength and stiffness of mechanical connections. Generally, the higher the specific gravity of the lumber (i.e. the denser the lumber), the stiffer and stronger the mechanical connections. For this reason, three different grade/species of lumber were used in connection tests: 1950f-1.7E Southern Pine, No. 2 Southern Pine, and No. 2 Spruce-PineFir.

Nine 14-foot long nominal 2- by 6-inch pieces of each lumber grade/species were obtained for this study. The nine pieces were nail-laminated to form three 14 -foot long, three-ply assemblies of each lumber grade/species. Each of these assemblies was then loaded to a total load, $\boldsymbol{P}$, of 3000 lbf using the $1 / 3$ point loading arrangement shown in Figures D. 2 and D.3.


Figure D.2. Load configuration for tests used to determine lumber modulus of elasticity.


Figure D.3. Test set-up for determination of lumber modulus of elasticity.

Load-head rate was fixed at 0.2 inches/minute with midspan displacements measured using a wire deflectometer. The wire deflectometer consisted of two spring-tensioned piano wires (one on each side of the assembly) whose ends were anchored on the neutral axis of the assembly at points directly above the support reactions. The vertical movement of the assembly relative to each wire was measured with a linear variable differential transformer (LVDT).

Ratios of applied load, $\boldsymbol{P}$, to midspan deflection, $\Delta$, were determined by linear regression of all data collected between 300 and 3000 lbf of applied force. These ratios were then substituted into the following equation to determine the apparent modulus of elasticity, $\boldsymbol{E}_{l}$ of the lumber:

$$
\begin{equation*}
\boldsymbol{E}_{l}=(\boldsymbol{P} / \Delta)\left(3 a L^{2}-4 a^{3}\right) /\left(4 b h^{3}\right) \tag{D.1}
\end{equation*}
$$

Where:

$$
\begin{aligned}
\boldsymbol{E}_{\boldsymbol{l}} & =\text { Apparent modulus of elasticity of lumber } \\
\boldsymbol{P} & =\text { Total load applied to the assembly } \\
\Delta & =\text { Deflection at midspan (relative to that at the supports) } \\
\boldsymbol{a} & =\text { Distance from reaction to nearest load point } \\
& =38 \text { inches } \\
\boldsymbol{L} & =\text { Span of beam } \\
& =114 \text { inches } \\
\boldsymbol{b} & =\text { Assembly width } \\
& =4.5 \text { inches } \\
\boldsymbol{h} & =\text { Assembly depth } \\
& =5.5 \text { inches }
\end{aligned}
$$

Resulting apparent modulus of elasticity values are tabulated in the right column of Table D.1. This table also contains moisture content, bulk density and specific gravity values which were calculated from measurements taken immediately after connection tests. Specifically, each threeply assembly was weighed and measured to determine its green mass and volume, respectively. Samples were then cut from each ply and oven-dried to determine their moisture content.

## Table D. 1 Properties Of Lumber Used In Connection Tests

| Lumber Species <br> and Grade | 3-Ply <br> Assembly <br> Number | Average <br> Moisture <br> Content, <br> percent <br> dry basis | Wet Bulk <br> Density*, <br> lbm/ft ${ }^{3}$ | Dry Bulk <br> Density*, <br> lbm/ft ${ }^{3}$ | Specific <br> Gravity, based <br> on oven dry <br> weight and <br> green volume | Apparent <br> Modulus of <br> Elasticity, <br> lbf/in |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Spruce-Pine-Fir | 1 | 10.35 | 33.4 | 30.2 | 0.484 | $1.91 \mathrm{E}+06$ |
| No. 2 | 2 | 10.31 | 28.6 | 25.9 | 0.415 | $1.72 \mathrm{E}+06$ |
| Southern Pine | 3 | 10.62 | 30.3 | 27.4 | 0.439 | $1.89 \mathrm{E}+06$ |
| No.2 | 2 | 5.71 | 31.3 | 29.6 | 0.475 | $1.64 \mathrm{E}+06$ |
| Southern Pine | 1 | 5.93 | 30.9 | 29.2 | 0.467 | $1.55 \mathrm{E}+06$ |
| 1950f 1.7E | 2 | 10.2 | 38.3 | 34.9 | 0.560 | $2.42 \mathrm{E}+06$ |

[^3]
## D. 3 Connection Test Methods and Equipment

Each 3-ply assembly was cut at midspan and then spliced back together with a pair of steel brackets that had been welded together using special steel splice plates. These specimens were then loaded to failure using the $1 / 3$ point loading arrangement shown in Figures D. 4 and D.5. Load-head rate was fixed at 0.2 inches/minute. The same wire deflectometers used to measure the midspan deflection in the MOE tests (see Figure D.3) were used to monitor the vertical displacement of the center of the steel bracket.


Figure D.4. Load configuration for tests used to determine lumber modulus of elasticity.


Figure D.5. Bolted connection prior to testing showing placement of wire deflectometers (left) and combo connection (connection with bolts and SDS screws) at maximum load (right).

Each 3-ply nail-laminated assembly was used for two connection tests. This was accomplished by removing the fasteners and steel bracket after the first test, and joining together (with a new steel bracket and fasteners) what were the two extreme ends of the bolted assembly during the first test. Using the same 3-ply nail-laminated assembly in two different connection tests resulted in better accounting of differences in connection behavior resulting from changes in lumber properties. The experimental design for these connection tests is summarized in Table D.2. This table
identifies the two connection test specimens made from each 3-ply assembly. Note that each connection test specimen is denoted with a three character ID. The first character is a "B", "S" or " C " and identifies the connection as either a bolted, screwed or combination bolt/screw connection, respectively. The second character is an "L", "M" or "H" and designates low, medium or high specific gravity lumber, respectively, which in turns denotes No. 2 SPF, No. 2 SP, and 1950 f 1.7E SP, respectively. The last character (a 1,2 or 3 ) is the number of the 3-ply lumber assembly used to fabricate the connection specimen.

## Table D. 2 Experimental Design for Connection Tests

| Lumber Species <br> and Grade | 3-Ply <br> Assembly <br> Number | Specimen Identification |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Bolted Connection | Screwed <br> Connection | Combo Connection |  |
| Spruce-Pine-Fir | 1 | BL1 | SL1 | CL2 |
| No. 2 | 2 | BL2 | SL3 | CL3 |
| Southern Pine | 1 |  | SM1 | CM1 |
| No.2 | 2 | BM2 | CM2 |  |
| Southern Pine | 1 | BM3 | SM3 |  |
| 1950f 1.7E | 2 | BH1 | SH1 | CH2 |

## D. 4 Results

The maximum bending moment sustained by each connection (i.e., midspan bending moment at failure) is given in Table D.3. These values were obtained by multiplying $1 / 2$ the maximum applied load by the distance between a support and nearest load point ( 38 inches). Figure D. 6 contains a plot of total applied load versus midspan deflection for each of the 18 assembly tests.
Table D. 3 Midspan Bending Moment at Failure

| Lumber Species <br> and Grade | 3-Ply <br> Assembly <br> Number | Bolted <br> Connection | Screwed <br> Connection | Combination <br> Connection | Average* |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 51870 | 77650 |  | 53310 |

[^4]

Figure D.6. Midspan deflection as a function of total applied load for each of the 18 connection test specimens.

One of the primary purposes for conducting the connection tests was to determine the relationship between the bending moment applied to the connection and the corresponding rotation between the bracket and wood post. Moment-rotation relationships can be obtained from the applied load versus midspan deflection plots using the lumber modulus of elasticity values in Table D. 1 and by assuming (1) no deformation of the steel bracket, and (2) that both halves of each connection behave identically during testing. The assumption of zero bracket deformation is sound because of the manner in which the brackets were fabricated for this series of tests, and because of the negligible strain in the steel under the loads to which the brackets were subjected. The assumption that both halves of each connection behave identically is very reasonable at low load levels and generally good up until the point of a wood or fastener failure. Once a failure occurs, there is likely to be considerably more deformation (i.e., rotation) associated with that half of the connection in which the failure occurred. The second photograph in Figure D. 5 illustrates the asymmetrical joint rotation that occurs once a wood or fastener failure occurs.

With the preceding assumptions, the total midspan deflection measured during the tests can be broken into two components, that due to rotation at the connections and that due to bending of the lumber. These two components of deflection are illustrated and identified in Figure D. 7 as $\Delta_{r}$ and $\Delta_{w}$, respectively.


Figure D.7. Components of total midspan deflection include (b) that due to rotation at the connection, $\Delta_{r}$, and (c) that due to bending strain in the lumber, $\Delta_{w}$.

The two components of total midspan displacement are calculated as:

$$
\begin{align*}
& \Delta_{r}=\boldsymbol{\theta} \boldsymbol{D}  \tag{D.2}\\
& \Delta_{\boldsymbol{w}}=\left(\boldsymbol{P} / \boldsymbol{E}_{l}\right)\left(3 \boldsymbol{a} \boldsymbol{L}_{\mathrm{e}}{ }^{2}-4 \boldsymbol{a}^{3}\right) /\left(4 \boldsymbol{b} \boldsymbol{h}^{3}\right) \tag{D.3}
\end{align*}
$$

Where:

$$
\begin{aligned}
\Delta_{r} & =\text { Midpsan deflection due to joint rotation } \\
\boldsymbol{\theta} & =\text { Joint rotation } \\
\boldsymbol{D} & =\text { Distance from support to center of joint rotation } \\
& =49.5 \text { inches } \\
\Delta_{w} & =\text { Midspan deflection due to bending of wood posts } \\
\boldsymbol{E}_{\boldsymbol{l}} & =\text { Apparent modulus of elasticity of lumber } \\
\boldsymbol{P} & =\text { Total load applied to the assembly } \\
\boldsymbol{a} & =\text { Distance from reaction to nearest load point } \\
& =38 \text { inches } \\
\boldsymbol{L}_{\boldsymbol{e}} & =\text { Effective bending span of 3-ply assembly (total assembly length minus effective } \\
& =99 \text { lenth of steel bracket) } \\
\boldsymbol{b} & =\text { Assembly width } \\
& =4.5 \text { inches } \\
\boldsymbol{h} & =\text { Assembly depth } \\
& =5.5 \text { inches }
\end{aligned}
$$

Because the joint region is in a shear-free region, the center of rotation between each half of the steel bracket and the corresponding section of the 3-ply assembly will be located at the centroid of the fastener pattern. These centroids are 7.5 inches from the midspan of the test specimens, or distance $\boldsymbol{D}$ of 49.5 inches from each support.
Joint rotation, $\boldsymbol{\theta}$, can be calculated be rearranging equation D. 2 and equating $\Delta_{r}$ to the difference between total midspan deflection, $\Delta_{t}$, and $\Delta_{w}$. In equation form:

$$
\begin{equation*}
\boldsymbol{\theta}=\left[\Delta_{t}-\left(\boldsymbol{P} / \boldsymbol{E}_{l}\right)\left(3 \boldsymbol{a} \boldsymbol{L}_{\mathrm{e}}{ }^{2}-4 \boldsymbol{a}^{3}\right) /\left(4 \boldsymbol{b} \boldsymbol{h}^{3}\right)\right] / \boldsymbol{D} \tag{D.4}
\end{equation*}
$$

Equation D. 4 was used to convert total applied load versus total midspan deflection data to bending moment versus joint rotation data. A portion of this data is compiled in Table D. 4 for each test specimen. Average values for each of the three connection types are also compile in Table D. 4 and have been plotted in Figure D.8.

Lumber specific gravity values are also tabulated in Table D.4. To determine if specific gravity had a measurable impact on joint stiffness, the specific gravity values were plotted against the bending moment at a rotation of 0.002 (Figure D.9). This plot does not show a strong relationship between specific gravity and joint stiffness for any of the connection types. This was expected given (1) the small range in specific gravity values, and (2) the high variability in joint stiffness (as indicated by the relatively high COV values in Table D.4).

Table D. 4 Joint Bending Moment-Rotation Data

| Specimen ID | Lumber Specific Gravity | Bending Moment, inch-lbf for Rotation in Radians of |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0.001 | 0.002 | 0.003 | 0.004 | 0.005 | 0.006 | 0.007 | 0.008 | 0.010 | 0.020 |
| SL1 | 0.484 | 8416 | 14992 | 19381 | 22759 | 26081 | 29052 | 31639 | 34026 | 38654 | 60083 |
| SL3 | 0.439 | 6026 | 11581 | 15925 | 18662 | 20867 | 22566 | 23849 | 25291 | 28042 | 41689 |
| SM1 | 0.475 | 12405 | 17590 | 20746 | 23136 | 25508 | 27130 | 28384 | 29231 | 31162 | 43050 |
| SM3 | 0.483 | 7782 | 13953 | 18936 | 23672 | 27464 | 30597 | 33194 | 35692 | 36320 | 54621 |
| SH1 | 0.560 | 3879 | 7923 | 11272 | 14102 | 16941 | 19726 | 22524 | 25224 | 31090 | 60535 |
| SH3 | 0.492 | 7496 | 14128 | 19287 | 22849 | 26038 | 28353 | 30457 | 32141 | 35251 | 44749 |
| Average | 0.489 | 7667 | 13361 | 17591 | 20863 | 23817 | 26237 | 28341 | 30268 | 33420 | 50788 |
| COV (\%)* | 8.1 | 36.9 | 24.6 | 19.8 | 18.1 | 17.0 | 16.0 | 15.2 | 14.7 | 11.9 | 17.1 |
| BL1 | 0.484 | 4089 | 8338 | 11783 | 15392 | 18285 | 20495 | 22398 | 24444 | 28039 | 39222 |
| BL2 | 0.415 | 3532 | 7065 | 10233 | 13401 | 15820 | 17613 | 19152 | 20764 | 23759 | 35702 |
| BM2 | 0.467 | 2327 | 4653 | 6980 | 9241 | 11024 | 12606 | 13937 | 15269 | 17348 | 27172 |
| BM3 | 0.483 | 2370 | 4739 | 7109 | 9567 | 11131 | 12341 | 13147 | 13784 | 14657 | 22535 |
| BH1 | 0.560 | 3948 | 7825 | 10803 | 12920 | 14659 | 16264 | 17456 | 18677 | 20647 | 31153 |
| BH2 | 0.537 | 2629 | 5257 | 8005 | 9990 | 11710 | 13231 | 14544 | 15630 | 17889 | 24888 |
| Average | 0.491 | 3149 | 6313 | 9152 | 11752 | 13772 | 15425 | 16772 | 18095 | 20390 | 30112 |
| COV (\%)* | 10.5 | 25.5 | 25.8 | 22.4 | 21.4 | 21.6 | 21.2 | 21.3 | 22.2 | 23.9 | 21.5 |
| CL2 | 0.415 | 5752 | 10965 | 15049 | 18534 | 22002 | 24945 | 27455 | 29914 | 33499 | 42313 |
| CL3 | 0.439 | 6210 | 11732 | 15523 | 18638 | 21519 | 24248 | 26623 | 28580 | 32679 | 42823 |
| CM1 | 0.475 | 5079 | 10405 | 14857 | 19140 | 23073 | 26904 | 30359 | 33572 | 39541 | 42506 |
| CM2 | 0.467 | 8363 | 13995 | 17333 | 19855 | 22059 | 24041 | 25692 | 26904 | 29049 | 45205 |
| CH2 | 0.537 | 7931 | 13098 | 17224 | 21350 | 25014 | 27937 | 30271 | 32252 | 36478 | 57196 |
| CH3 | 0.492 | 6261 | 11966 | 15807 | 18774 | 21225 | 22965 | 24347 | 26095 | 29691 | 48319 |
| Average | 0.471 | 6599 | 12027 | 15966 | 19382 | 22482 | 25173 | 27458 | 29553 | 33490 | 46394 |
| COV (\%)* | 9.0 | 19.4 | 11.1 | 6.7 | 5.6 | 6.2 | 7.5 | 8.9 | 10.0 | 12.0 | 12.4 |

COV (coefficient of variation) in $\%=100$ (Standard Deviation of Values)/(Average of Values)


Figure D.8. Average joint bending moment-rotation curves for the three connection types.


Figure D.9. Relationships between lumber specific gravity values and test specimen bending moments at a joint rotation of 0.002 .

## D. 5 Fastener Shear Strength and Load-Slip Relationships

A joint located in a zone of constant bending moment and no shear will rotate about the centroid of the fastener pattern. For the joints in this study, this point is located midway between the centroid of the two fastener patterns as shown in Figure D.10. From the free body diagram in Figure D.10, it is evident that the shear force, $\boldsymbol{F}$, in each fastener pattern in numerically equal to the bending moment divided by 8.50 inches. It is also evident from Figure D. 10 that the average interlayer slip (i.e., movement between the wood and steel bracket) at the center of each fastener pattern is equal to the product of the rotation and 4.25 inches.


Figure D.10. Average shear force, $\boldsymbol{F}$, acting on each fastener pattern is numerically equal to the applied bending moment, $\boldsymbol{M}$, divided by 8.50 inches.

Dividing bending moments by 8.5 inches and multiplying rotations by 4.25 inches yields the interlayer slips and shear forces appearing in Table D.5. Note that shear forces in columns 1, 2 and 3 columns are calculated from the average bending moment in the bolt, screw, and combination connections, respectively. Values in column 4 were obtained by divided values in column 2 by six. Values in column 5 were obtained by doubling the values in column 4 and adding the sum to the values in column 1. Table D. 5 data is graphically illustrated in Figure D.11.
Table D. 5 Fastener Shear Force As A Function of Interlayer Slip

| Interlayer Slip, inches | Shear Force, lbf |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Single Bolt in Double Shear (1)* | Six Screws in Single Shear (2)* | Single Bolt in Double Shear plus Two Screws in Single Shear (3)* | One Screw in Single Shear (4)* | Single Bolt in Double Shear plus Two Screws in Single Shear (5)* |
| 0.0043 | 370 | 902 | 776 | 150 | 671 |
| 0.0085 | 743 | 1572 | 1415 | 262 | 1267 |
| 0.0128 | 1077 | 2070 | 1878 | 345 | 1767 |
| 0.0170 | 1383 | 2455 | 2280 | 409 | 2201 |
| 0.0213 | 1620 | 2802 | 2645 | 467 | 2554 |
| 0.0255 | 1815 | 3087 | 2962 | 514 | 2844 |
| 0.0298 | 1973 | 3334 | 3230 | 556 | 3085 |
| 0.0340 | 2129 | 3561 | 3477 | 593 | 3316 |
| 0.0383 | 2270 | 3778 | 3719 | 630 | 3530 |
| 0.0425 | 2399 | 3932 | 3940 | 655 | 3709 |
| 0.0468 | 2475 | 4127 | 4124 | 688 | 3851 |
| 0.0510 | 2561 | 4287 | 4333 | 714 | 3990 |
| 0.0553 | 2642 | 4511 | 4445 | 752 | 4146 |
| 0.0595 | 2735 | 4748 | 4543 | 791 | 4318 |
| 0.0638 | 2866 | 4974 | 4765 | 829 | 4523 |
| 0.0680 | 3023 | 5172 | 4869 | 862 | 4747 |
| 0.0723 | 3162 | 5406 | 4949 | 901 | 4964 |
| 0.0765 | 3256 | 5580 | 5132 | 930 | 5116 |
| 0.0808 | 3407 | 5773 | 5261 | 962 | 5331 |
| 0.0850 | 3543 | 5975 | 5458 | 996 | 5534 |
| 0.0893 | 3679 | 6128 | 5641 | 1021 | 5722 |
| 0.0935 | 3813 | 6289 | 5835 | 1048 | 5909 |
| 0.0978 | 3941 |  | 5965 |  |  |
| 0.1020 | 4028 |  | 6052 |  |  |
| 0.1063 | 4085 |  | 6133 |  |  |
| 0.1105 | 4143 |  | 6280 |  |  |
| Maximum Shear Force | 5810 | 7650 | 7460 | 1275 | 8360 |

* Values in columns 1, 2 and 3 are for bolt, screw, and combination connections, respectively. Values in column 4 were obtained by divided values in column 2 by six. Values in column 5 were obtained by doubling column 4 values and adding the sum to the values in column 1 .


Figure D.11. Graphically display of shear force - interlayer slip data from Table D.5. Numbers in label boxes correspond to Table D. 5 column numbers.

The data in Table D. 5 and plot in Figure D. 11 demonstrate that the stiffness of a connection comprised of a combination of bolts and screws can be predicted using stiffness data for a single bolt plus stiffness data for a single screw.

Since being able to predict connection stiffness is fundamental to modeling connections, leastsquare linear regression was used to determine the initial slope of the shear-load versus interlayer slip relationship for a single bolt in double shear (column 1 of Table D.5) and for a single screw in single shear (column 4 of Table D.5). Only data points up to a slip of 0.013 inches were used in the regressions. These analyses provided the following interlayer shear stiffness values:

## Interlayer Shear Stiffness Values

0.5 -inch diameter SAE grade 5 bolt in double shear $=85,500 \mathrm{lbf} / \mathrm{inch}$
0.25 - by 3.0-inch Simpson Strong-Drive ${ }^{\circledR}$ wood screw in single shear $=28,700 \mathrm{lbf} /$ inch

The Wood Handbook (FPL, 1999) recommends an interlayer shear stiffness in lbf/inch for bolts or lag screws in wood-to-metal connections of $270,000 \boldsymbol{D}^{1.5}$ where $\boldsymbol{D}$ is the fastener diameter in inches. This equation yields $95,460 \mathrm{lbf} / \mathrm{inch}$ for a 0.5 -inch diameter fastener and $33,750 \mathrm{lbf} / \mathrm{inch}$ for a 0.25 inch diameter fastener. These values are surprisingly close to those determined via regression analysis given the fact that such values are highly influenced by wood and fastener material properties, and in this study, by friction between the wood and steel brackets.

Table D. 5 shows average ultimate shear strengths of 5810 lbf for the 0.5 -inch diameter SAE grade 5 bolt in double shear, and 1275 lbf for the 0.25 - by 3.0 -inch Simpson Strong-Drive ${ }^{\circledR}$ wood screw in single shear. These values compare with calculated 10-minute ( $\boldsymbol{C}_{\boldsymbol{D}}=1.6$ ) NDS allowable stress design (ASD) values of approximately $1950 \mathrm{lbf}\left(1220 \mathrm{lbf} \times \boldsymbol{C}_{\boldsymbol{D}}=1.6\right)$ for the SAE grade 5 bolt and
approximately $450 \mathrm{lbf}\left(280 \mathrm{lbf}\right.$ x $\left.\boldsymbol{C}_{\boldsymbol{D}}=1.6\right)$ for the SDS screw. The calculated NDS values are approximately $35 \%$ of the average ultimate shear strengths.

The 10 -minute NDS ASD value of 450 calculated for the SDS screw is based on a shank diameter of 0.242 inches and a bending yield strength of $164,000 \mathrm{lbf} / \mathrm{in}^{2}$. This 10 -minute value is less than the normal load duration $\left(\boldsymbol{C}_{\boldsymbol{D}}=1.0\right)$ value of 470 lbf published by Simpson for the SDS screw when it is used to connect minimum 14 gage steel to Southern Pine or Douglas Fir. According to Mr. Aram Khachadourian of Simpson Strong-Tie Company, Inc., Simpson arrived at their higher design value by laboratory testing specimens in accordance with ASTM D1761. They then determined connection yield strengths by the $5 \%$ diameter offset method (using a root diameter of 0.185 inches), and divided this yield strength by a $\boldsymbol{K}_{\boldsymbol{D}}=10 \boldsymbol{D}+0.5=2.35$ to obtain the normal load duration (i.e., 10 year) design value (in this case, the $\boldsymbol{K}_{\boldsymbol{D}}$ value includes the safety factor and adjustment for load duration). This value was lower than the alternative method of dividing the mean ultimate load by a factor of safety of 2.0 and a load duration factor of 1.6. Using the same 0.185 inch diameter as Simpson produces a $5 \%$ diameter offset value of 545 lbf (Figure D.12) and a corresponding normal load duration value of 230 lbf for the SDS screw fasteners in this study. This value is less than half of that reported by Simpson. Note that dividing the mean ultimate load of 1275 lbf by a safety factor of 2.0 and load duration factor of 1.6 produces a normal load duration design value of 400 lbf which is much closer to Simpson's design value of 470 lbf .


Figure D.12. Determination of the 5\% diameter offset values for an SDS screw.

## D. 6 References

Forest Products Laboratory. 1999. Wood handbook--Wood as an engineering material. Gen. Tech. Rep. FPL-GTR-113. Madison, WI: U.S. Department of Agriculture, Forest Service, Forest Products Laboratory. 463 p.

## I．REVOLUTIONARY DESIGN

A．PERMA－COLUMNS are the first product to combine the economy of post－frame construction with the durablitity of a concrete foundation．
B．The exclusive design of the PERMA－COLUMN is patented．

## II．TECLHNICAL SPECIFICATIONS

A．The latest in SCC pre－casting technology creates a product with three times the strength of regular concrete．
B．Polymer fiber relinforcement and premfum grade steel reinforcement dramatically enhance flexural strength．
C．Corrosion inhibitors protect internal steel reinforcement．
D．Air entraining admixtures insure resistance to harsh freeze－ thaw cycles．

## III．INVESTMENT SECURITY

A．PERMA－COLUMNS ksep wood out of the ground ensuring that your building＇s foundation will never rot．
B．PERMA－COLUMNS protect your building investment by securing its value for a lifetime．

## IV．ENVIRONMENTAL SAFETY

A．PERMA－COLUMNS do not use the harsh chemicals found in treated lumber，which are being phased out by the EPA．
B．Using an environmentally frlendly product promotes peace of mind．

## V．STRENGTH DATA

A．PERMA－COLUMNS have been tested by The University of Wisconsin．Desisn manuals are available by request．
B．In comparative strength tests performed by Purdue University，PERMA－COLUNNS have proven to outperform the industry standard．


## 5 MロDELS Tロ MEET YロUR NEEDS



PC6300－for a 3 ply $2^{\prime \prime} \times 6^{n}$ Laminated wood column PC5 400 －for 14 ply $2^{\prime \prime} \times 6^{\prime \prime}$ laminated wood column PC6600－for a $6^{\prime \prime} \times 6^{\prime \prime}$ wood post replacement pceano－for a 3 ply $2^{\prime \prime}$ X $a^{\prime \prime}$ lamingted wood columin PCes 00 －for a 4 ply $2^{n} \times 8^{\prime \prime}$ laminated wood column Tonsile a dekty proferiknal for appropritate model．


[^0]:    Chart Assumptions
    Laminated wood portion transfers axial loads through direct bearing on steel seat plate
    Blank in chart represents deflection controls design, gray box indicates wood connection at steel bracket controls Final column design should include a complete building analysis by a Design Professional

[^1]:    * From AF\&PA 1996 Edition of Load and Resistance Factor Design Manual For Engineered Wood Construction. Assumes columns with full lateral bracing and only major axis bending
    ** Based on changes incorporated in 2001 Edition of Allowable Stress Design Manual for Engineering Wood Construction (AF\&PA, 2001).
    *** From ASAE EP559

[^2]:    * Specimens 5 and 6 fabricated with \#4 rebar.
    **5\% E. L. $=5 \%$ Exclusion limit assuming normal distribution $=$ Mean - Std Dev (1.645)

[^3]:    * Based on green volume

[^4]:    * Values in parentheses are sample standard deviation values

